



Adaptive Resolution Simulations: Towards Open Systems Molecular Dynamics Simulations

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Rutgers University * Dec. 19, 2010

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Support:

MMM Initiative of the MPG, Volkswagen Foundation, DAAD

Outline

- **Motivation: Soft and Nanostructured Matter**
- **AdResS: Adaptive Resolution MD Simulation**
 - Method, first Applications
 - Recent developments
- **Particle-Continuum: AdResS + Hybrid MD**
- **Conclusions/Outlook**

Soft Matter

“Soft” means:

- low energy density
- nanoscopic length scales ($10\text{\AA} \dots 1000\text{\AA}$)
- large fluctuations
- thermal energy $k_B T$
relevant energy scale

Energy Scale $k_B T$ for $T=300K$

$$E = 1.38 \cdot 10^{-23} \text{ J / K} \cdot 300 \text{ K}$$

$$kT \approx 4.1 \cdot 10^{-21} \text{ J}$$

$$kT \approx 2.5 \cdot 10^{-2} \text{ eV}$$

$$kT \approx 9.5 \cdot 10^{-4} E_H$$

$$kT \approx 4.1 \text{ pNnm}$$

$$kT \Rightarrow 200 \text{ cm}^{-1}$$

$$kT \Rightarrow 0.6 \text{ kcal / mol}$$

$$kT \Rightarrow 2.5 \text{ kJ / mol}$$

$$E \approx 3 \cdot 10^{-19} \text{ J} \approx 80 kT$$

$$E \approx 4 kT - 10 kT$$

Electronic structure, CPMD

Quantum Chemistry

Biophysics Membranes, AFM

Spectroscopy

Chemical Bond

Hydrogen Bond

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Electronic structure, QM

Quantum Chemistry

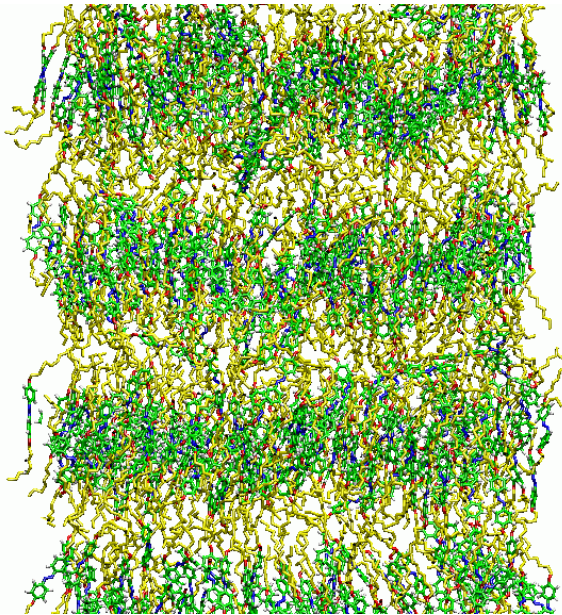
Biophysics Membranes, AFM

Spectroscopy

Green light photon $\approx 2\text{-}2.5 \text{ eV} \approx 100 \text{ kT}$

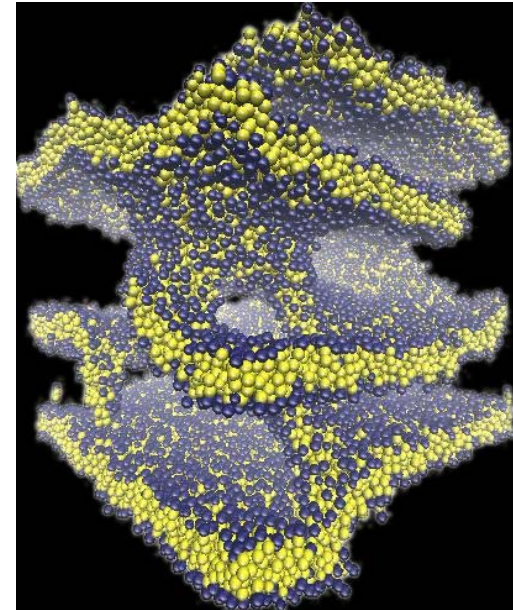
**Chemical Bond
Hydrogen Bond**

Soft Matter – Nanostructured Matter



Volume
 $V = L^3$

A: Surface and
Interface Area



Nanoscopically Structured Material: $V/A \ll 1\mu\text{m}$

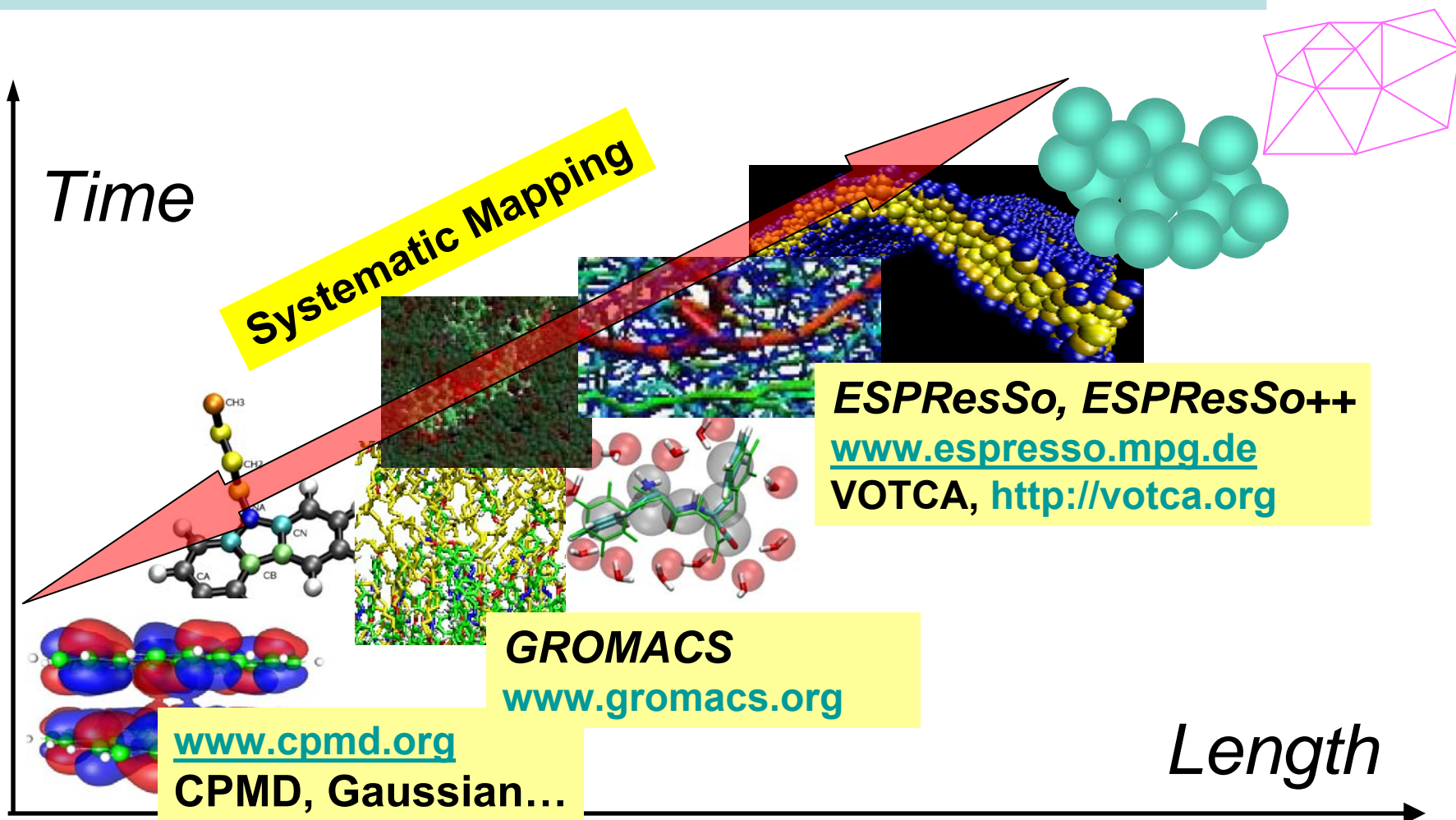
=>

Distinction Bulk vs Surface/Interface not useful

Definition of A usually depends on the question studied!

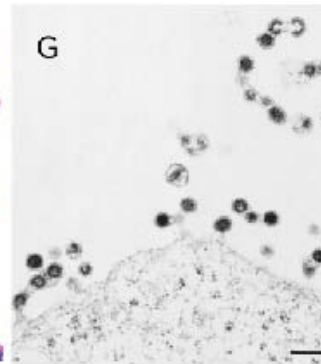
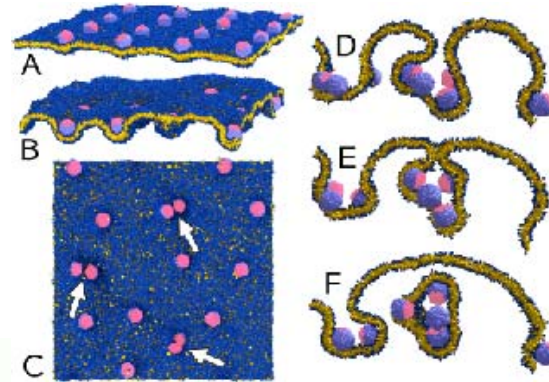
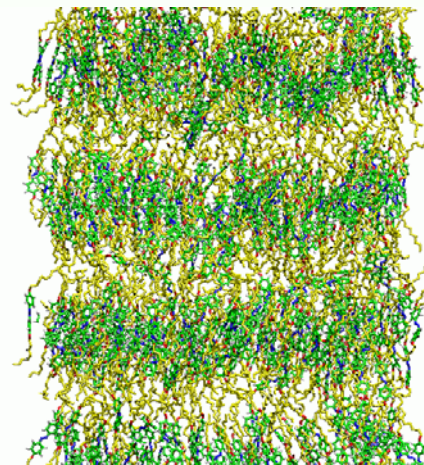
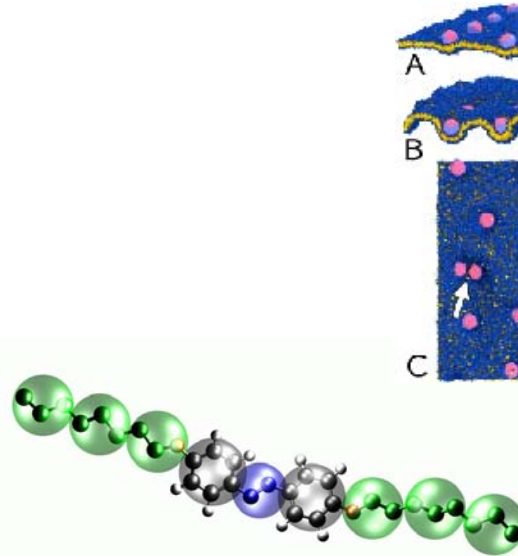
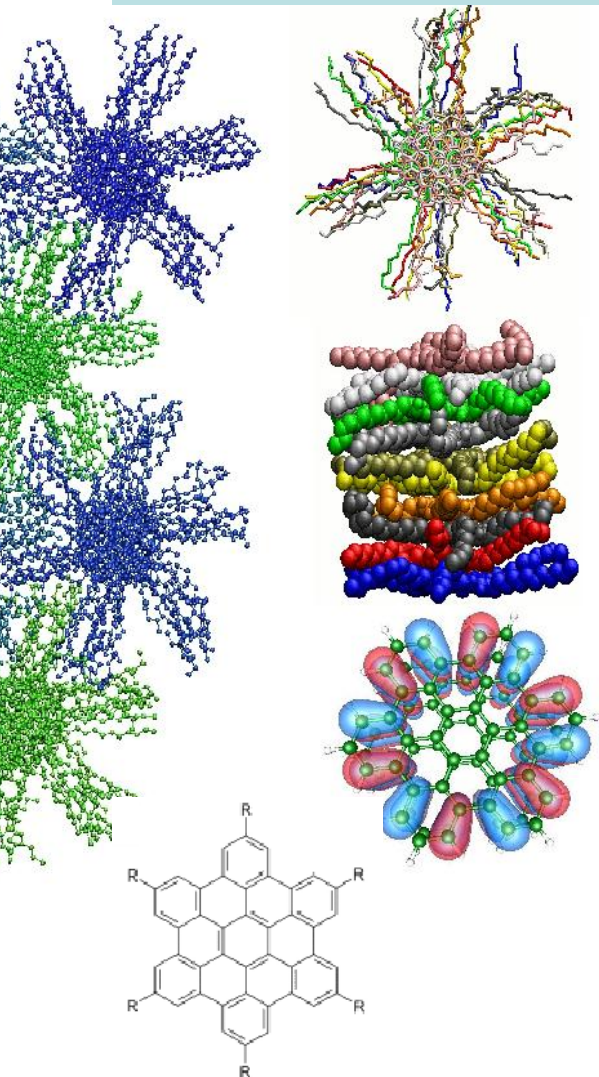


Characteristic Time and Length Scales



Local Chemical Properties	---	Scaling Behavior of Nanostructures
Energy Dominance	---	Entropy Dominance of Properties

Standard Approach: Run whole system on one level of resolution.

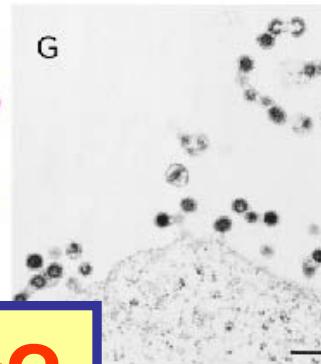
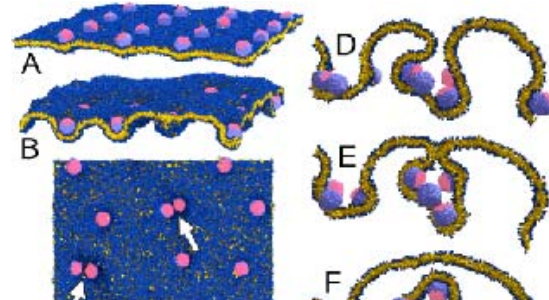
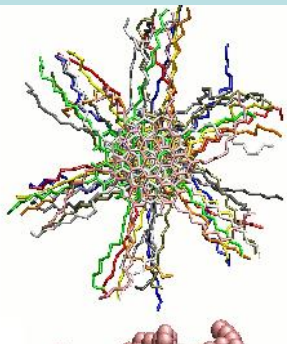
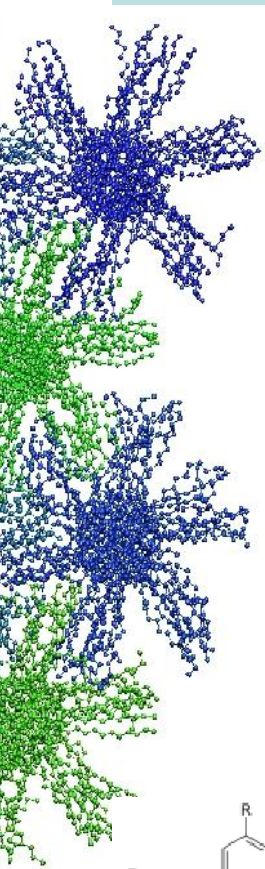


M. Deserno et al.,
Nature, 2007

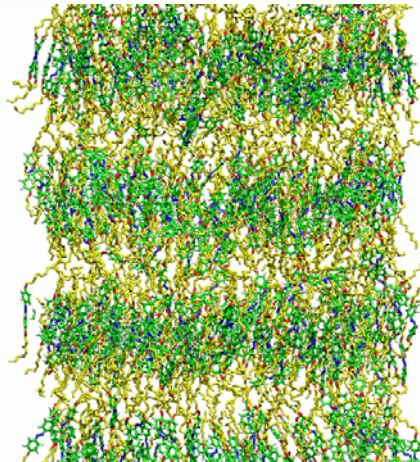
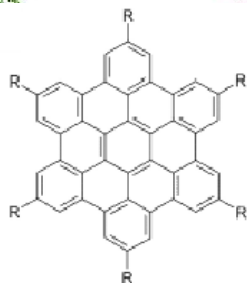
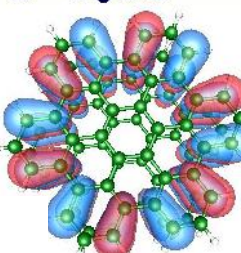
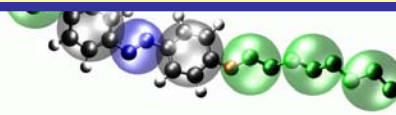
C. Peter et al, 2008ff

Andrienko et al,
PRL 98, 227402 (2007)

Standard Approach: Run whole system on one level of resolution.



Do we need/want to do that?



M. Deserno et al.,
Nature, 2007

Andrienko et al,
PRL 98, 227402 (2007)

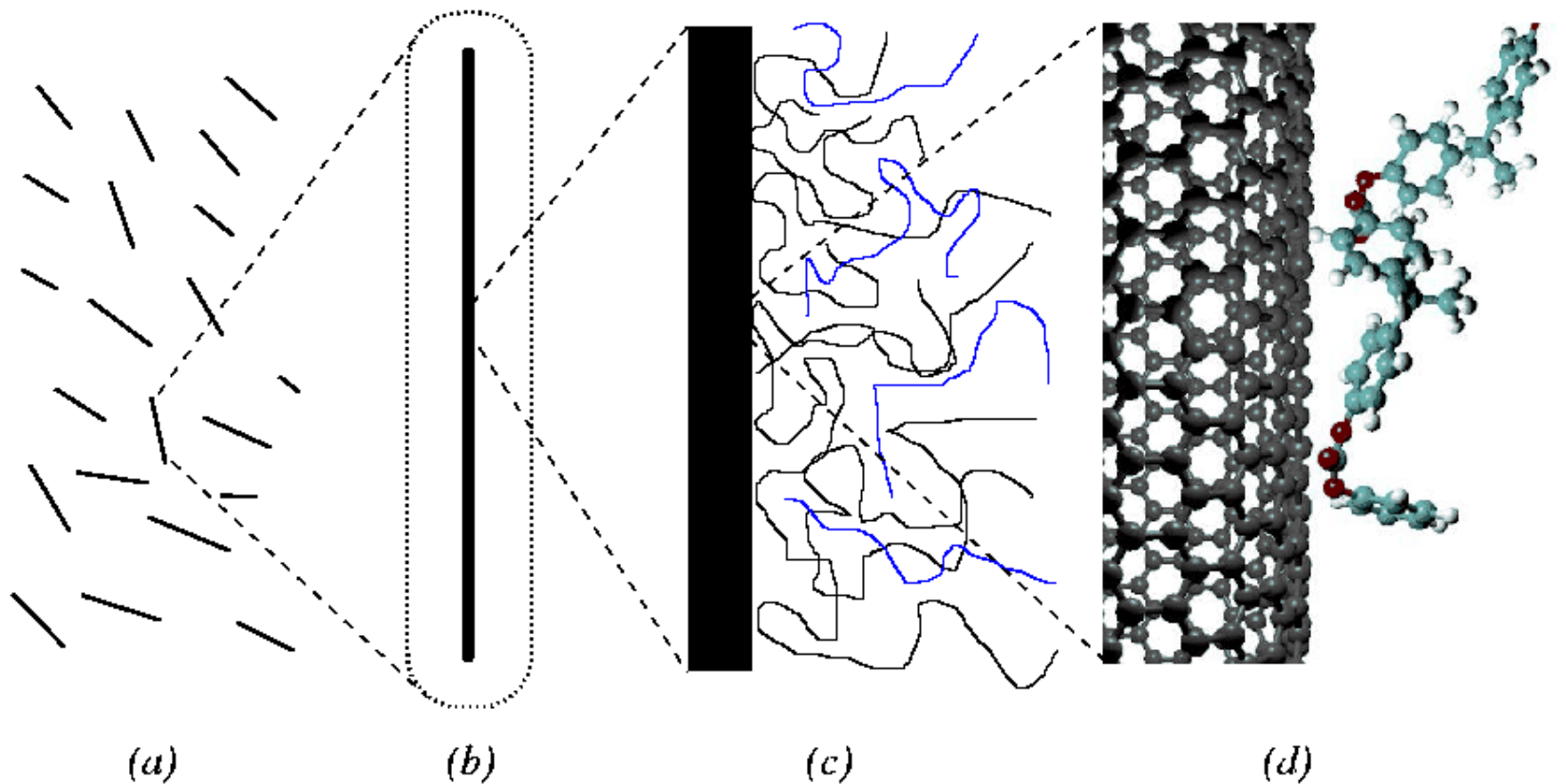
C. Peter et al, 2008ff

Outline

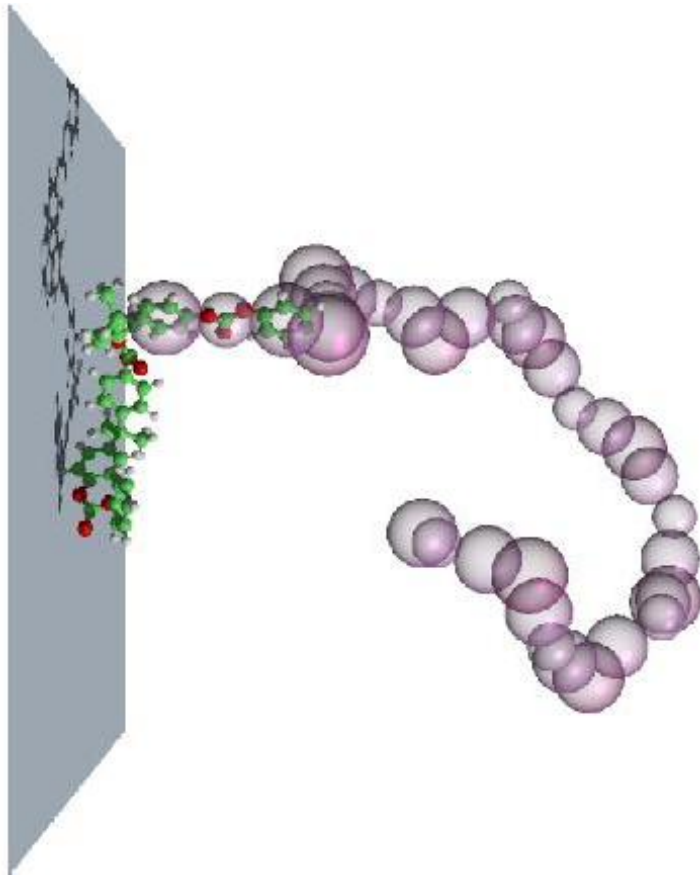
- Motivation: Soft and Nanostructured Matter
- **AdResS: Adaptive Resolution MD Simulation**
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 - Recent developments
- Particle-Continuum: AdResS + Hybrid MD
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Relevant Levels of Resolution

Example: Polymer/Nanotube Composites



Adaptive Inhomogeneous Coarse-Graining



Specific atomic-scale energetics dominant at surface

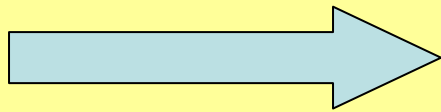
Molecule-scale entropy dominant in bulk

Coarsened fragments provide equilibrated “boundary conditions” for full-blown embedded atomistic simulation

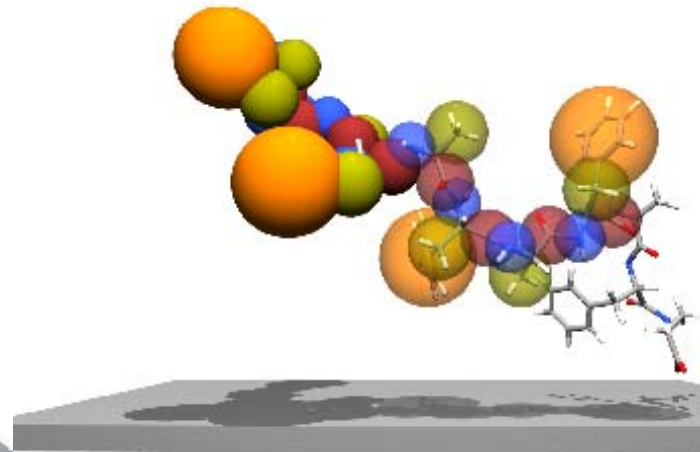
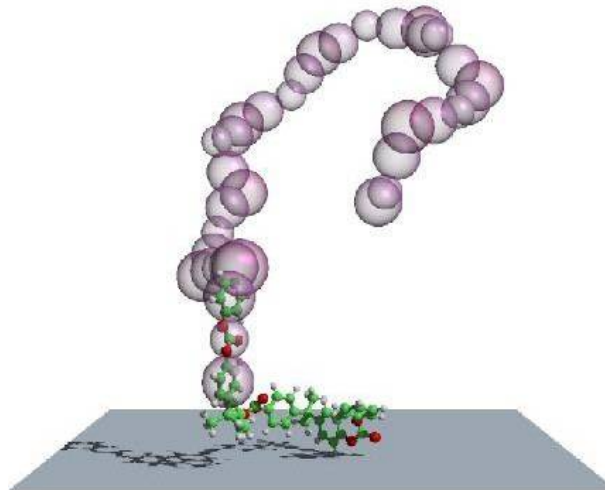
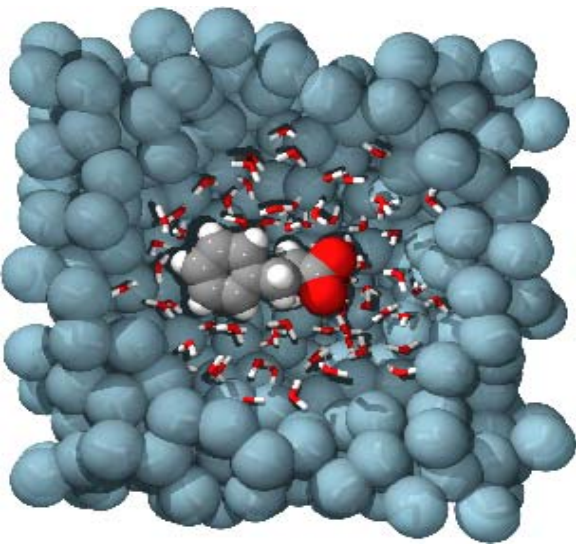
AdResS: **A**daptive **R**esolution **S**imulations

M. Praprotnik, L. Delle Site, KK, Ann. Rev. Phys. Chem. 2008, 59: 545-71

Free exchange of molecules/particles between regimes with different levels of resolution:

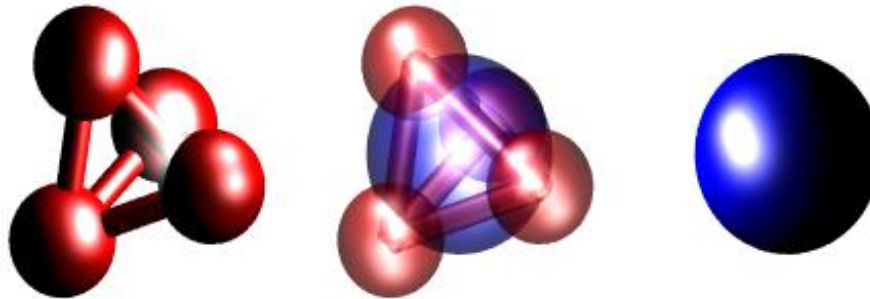


equilibrium between both regimes,
no kinetic barrier

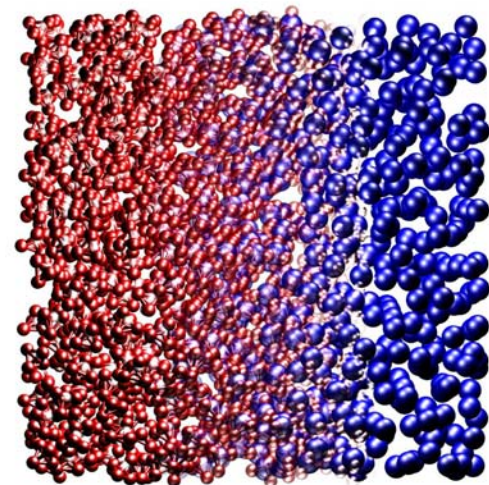


Adaptive Methods: Changing degrees of freedom on the fly

Adaptive multiscale method: Simple test case



Tetrahedron, repulsive LJ Particles, Sphere FENE bonds	↔	Hybrids	↔	“Softer”
Explicit Atom regime	↔	Transition regime	↔	Coarse Grained regime



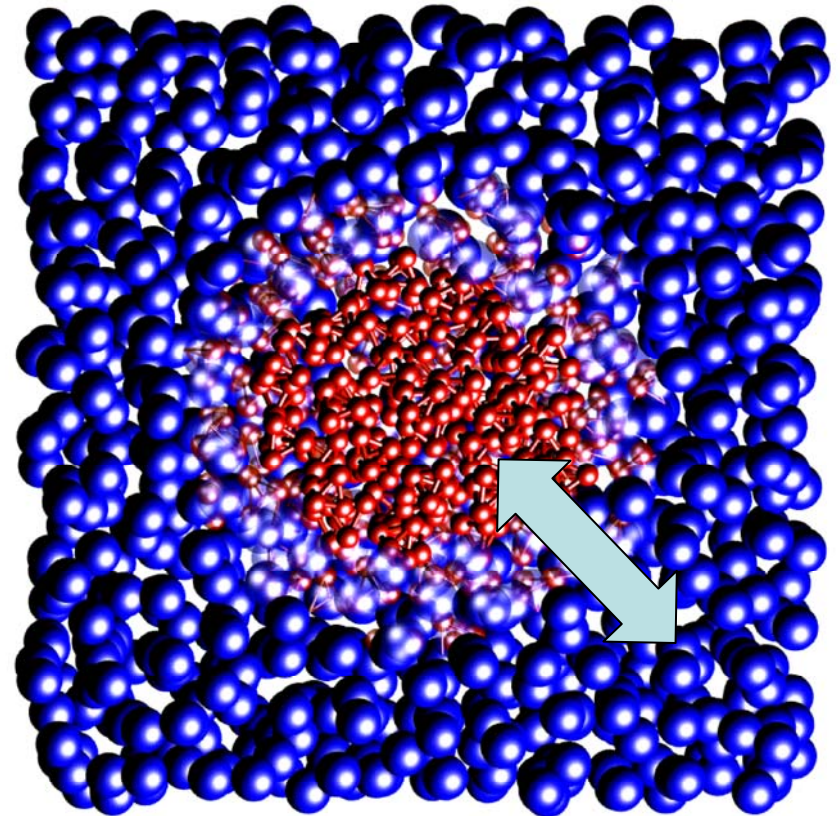
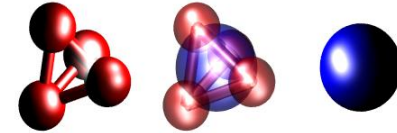
Adaptive Methods: Changing degrees of freedom (DOFs) on the fly

Requirements

- Same mass density
- Same Pressure (\Rightarrow Eq. of state)
- Same temperature

- Free exchange between regimes
- Same center-center $g(r)$

- Simple two body potential



Adaptive Methods: Changing degrees of freedom (DOFs) on the fly

Requirements

- Same mass density
- Same Pressure (\Rightarrow Eq. of state)
- Same temperature

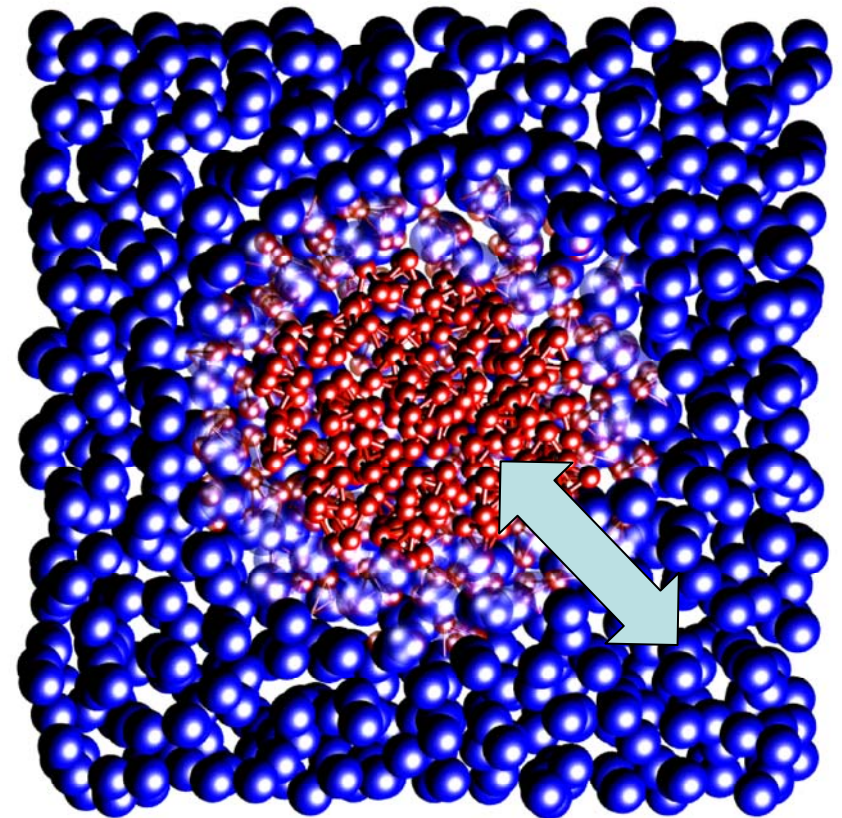
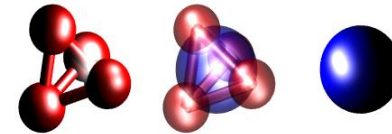
- Free exchange between regimes
- Same center-center $g(r)$

- Simple two body potential

\Rightarrow “Some similarities” to 1st order phase transition

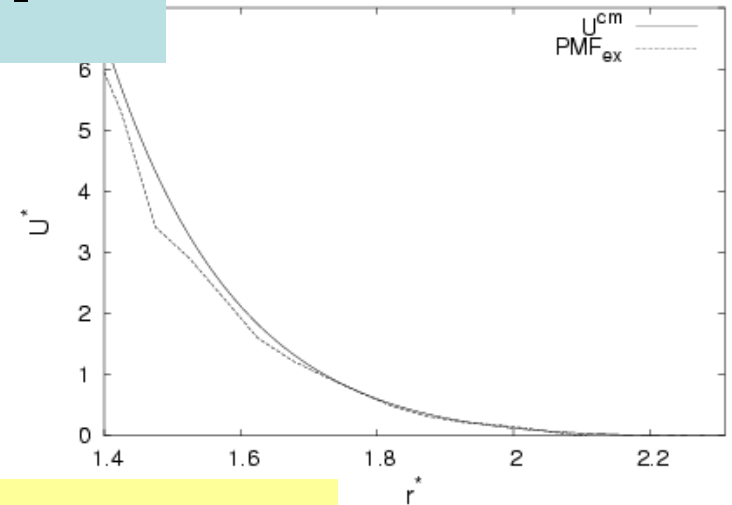
\Rightarrow Phase equilibrium

\Rightarrow Thermostat has to provide/take out latent heat due to change in degrees of freedom



Coarse Grained Model

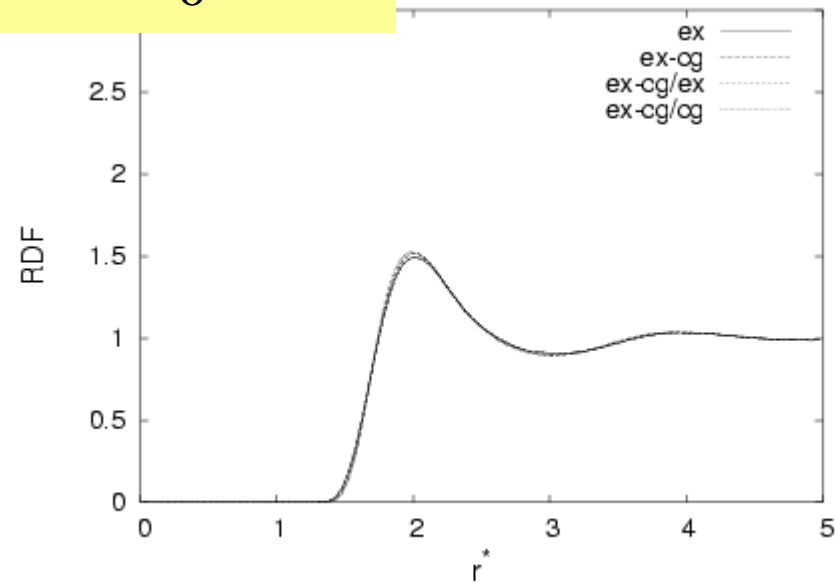
Study explicit atom and CG system
separately
=> fit CG Interaction Potential:



$$U^{cm}(r) = \gamma \{1 - \exp[-\kappa(r - r_0)]\}^2$$

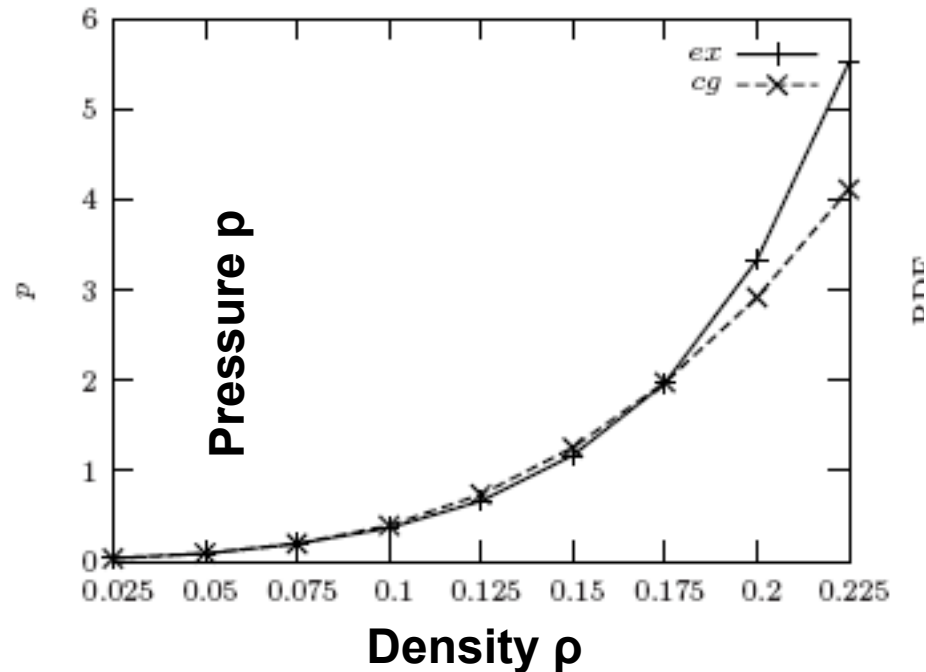


$$\mu_{ex} = \mu_{cg}, \quad p_{ex} = p_{cg}, \quad T_{ex} = T_{cg}$$



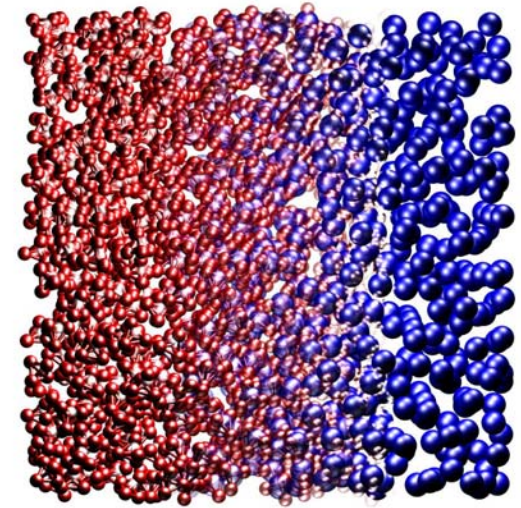
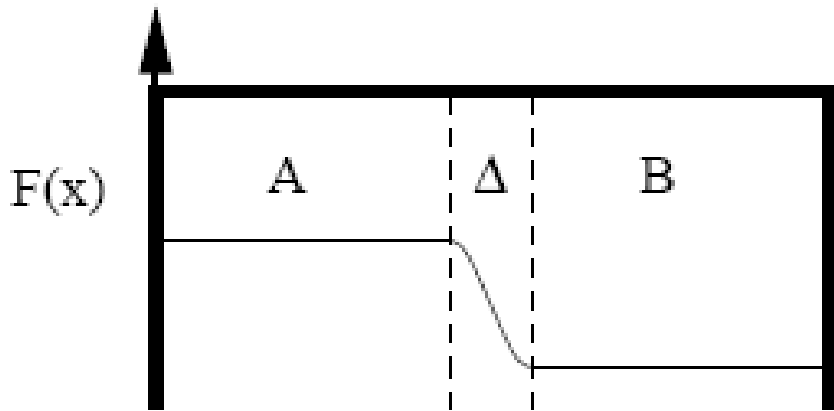
Initial General Considerations

$$\mu_{ex} = \mu_{cg}, \quad p_{ex} = p_{cg}, \quad T_{ex} = T_{cg}$$



(m) Equation of state for $\rho = 0.175$ and $T = 1$.

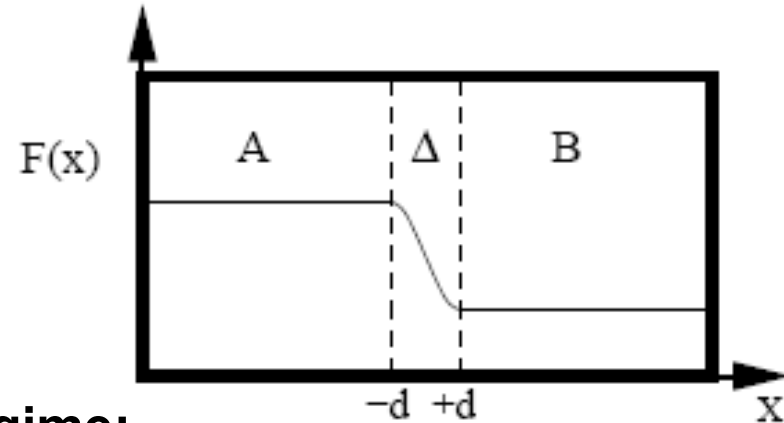
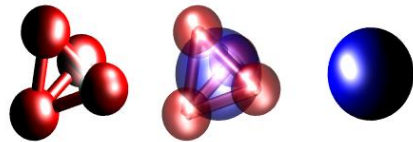
Transition Regime: Changing Degrees of Freedom (DOF): switching function $w(x)$ for DOFs



- The number of DOF is $n = n(x)$ with ; $n_A = \text{const}_A$; $n_B = \text{const}_B$; and $n_\Delta = n(x)$
- The system is in equilibrium which implies:
$$\lim_{x \rightarrow d^-} \frac{\partial F_A(x)}{\partial x} = \lim_{x \rightarrow d^+} \frac{\partial F_B(x)}{\partial x} = 0$$

Transition Regime: Changing Degrees of Freedom (DOF): switching function $w(x)$ for DOFs

$w=1$... $w=0$



Definition of Temperature in transition regime:

Fractional degrees of freedom, switching function $w(x)$

=> generalization of equipartition theorem

=> Defines thermostat to take out/in “latent heat of the DOFs”

$$dV_w = d^w q \Gamma(w/2) / 2\pi^{w/2} \Gamma(w) = |q|^{w-1} dq / \Gamma(w) = dq^w / w\Gamma(w)$$

$$\Rightarrow H(q) = q^n \quad \langle H(q) \rangle_w = \frac{w}{n} k_B T$$

w is the fractional dimension of DOF q , $w=1$ and $n=2$ standard case

Theoretical Basis: Temperature...

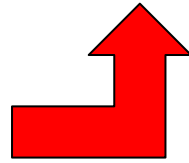
- Change resolution,
⇒ “Latent heat” of fading/emerging degrees of freedom (DOFs)
- Generalized Equipartition Theorem for DOFs with fractional dimension $w(x)$
⇒ Well defined temperature T in Δ , well defined thermostat
- Smooth switching region Δ with switching function $w(x)$
- Practical Implementation?

AdResS:

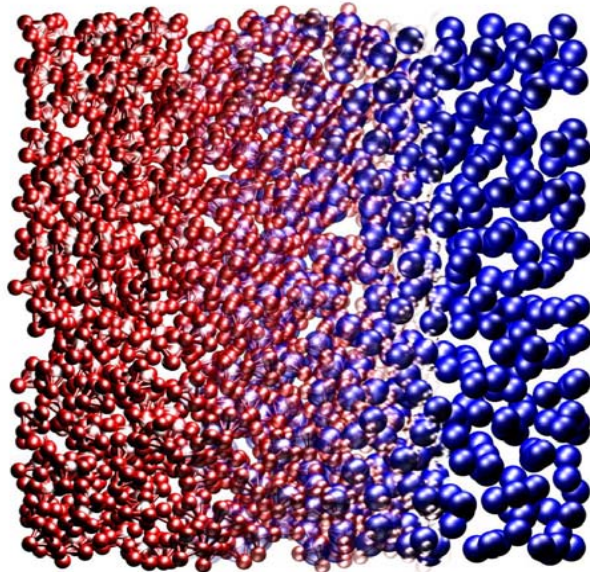
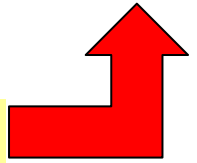
Transition Regime – Energy $U_{\alpha\beta}$ Interpolation?

$$U_{\alpha\beta} = w(X_{\alpha})w(X_{\beta})U_{\alpha\beta}^{atom} + [1 - w(X_{\alpha})w(X_{\beta})]U_{\alpha\beta}^{cg}$$

Full atomistic potential



Full coarse grained potential

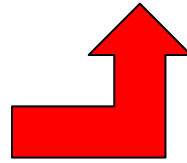


- Drift terms from $w(x)$
- Violation of Newton's 3rd law
- Mathematical inconsistencies at boundaries

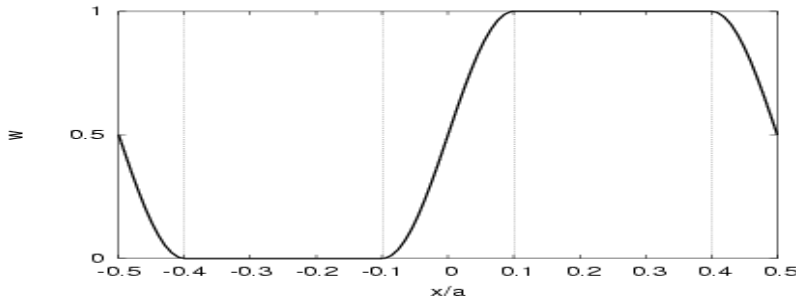
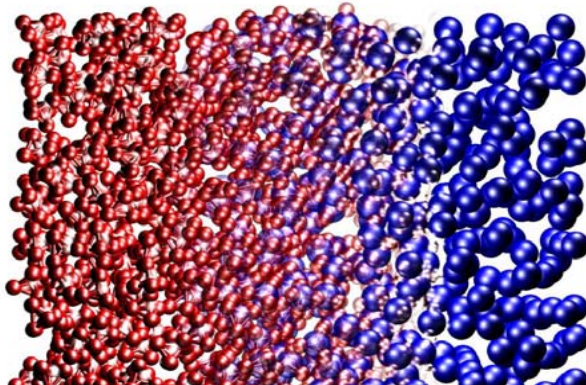
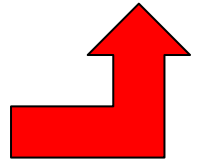
AdResS: Transition Regime - Force Interpolation

$$F_{\alpha\beta} = w(X_\alpha)w(X_\beta)F_{\alpha\beta}^{atom} + [1 - w(X_\alpha)w(X_\beta)]F_{\alpha\beta}^{cg}$$

Full atomistic force



Full coarse grained force



Interactions

explicit-explicit

CG-CG

hybrid-hybrid

CG- hybrid: CG-CG

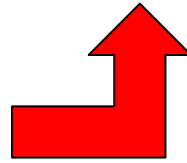
explicit-hybrid: explicit-explicit

AdResS:

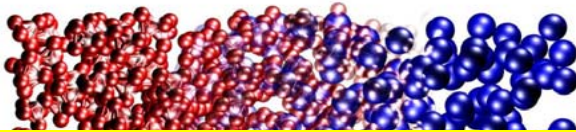
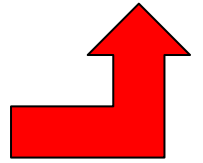
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Full atomistic force

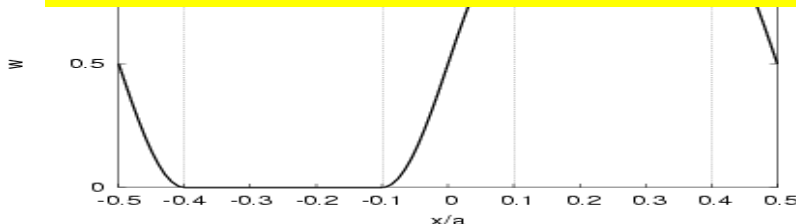


Full coarse grained force



***Transition regime: Force interpolation
(Newton's 3rd law fulfilled, no drift forces)***

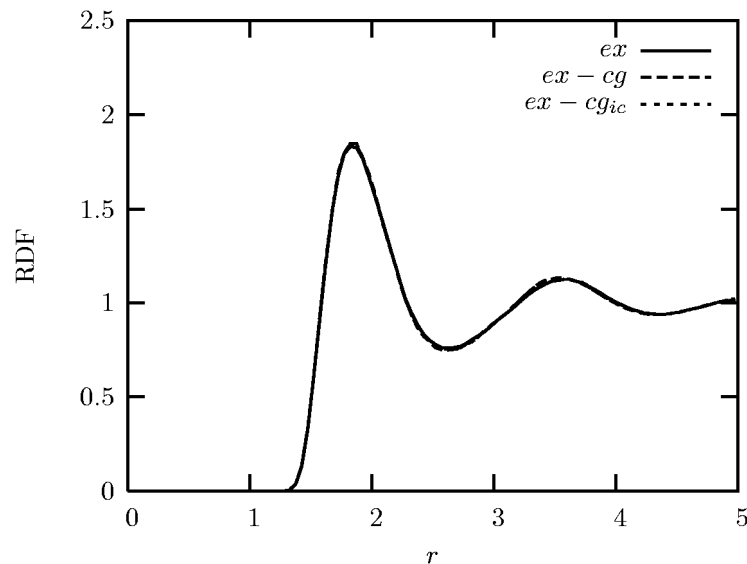
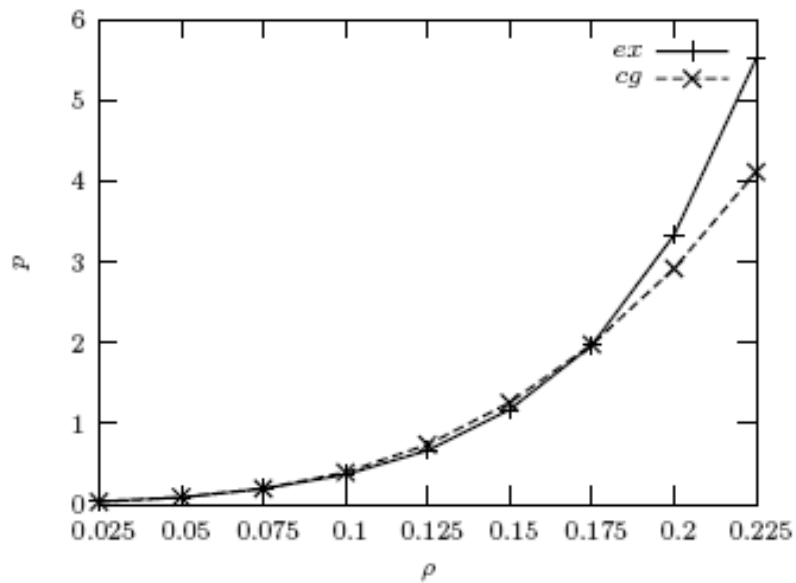
No transition energy function defined!



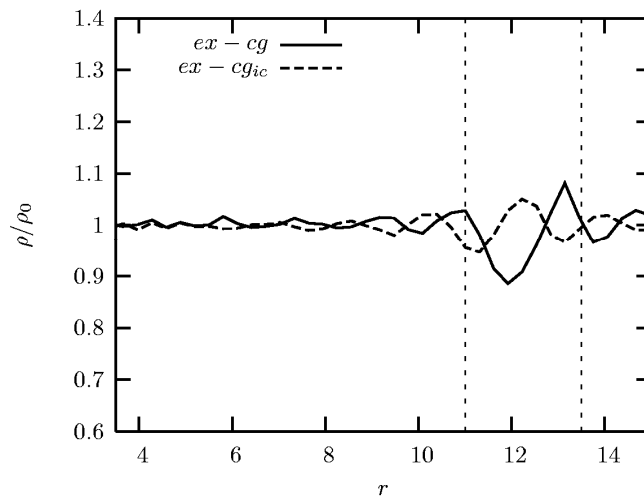
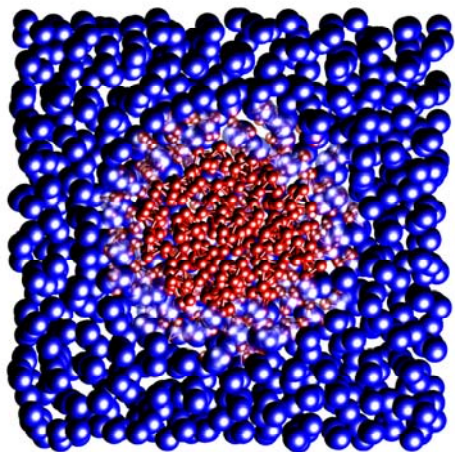
CG-hybrid: CG-CG

explicit-hybrid: explicit-explicit

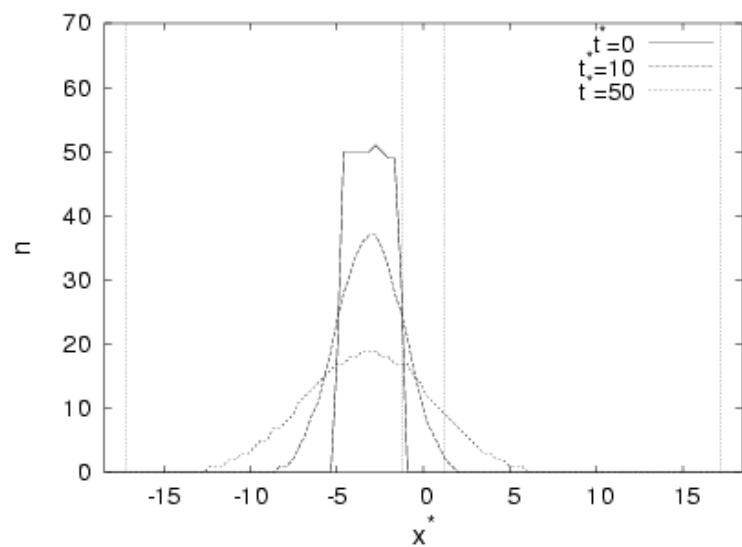
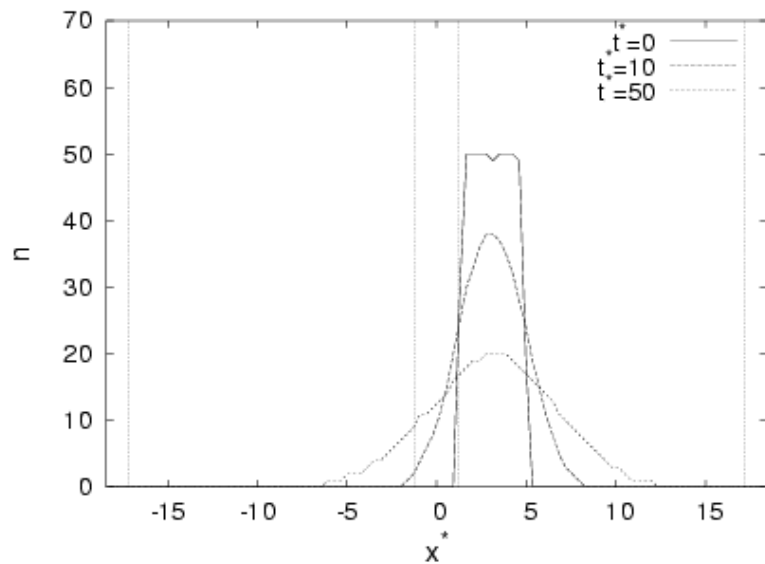
First Test: Radial Distributions, Densities, high density



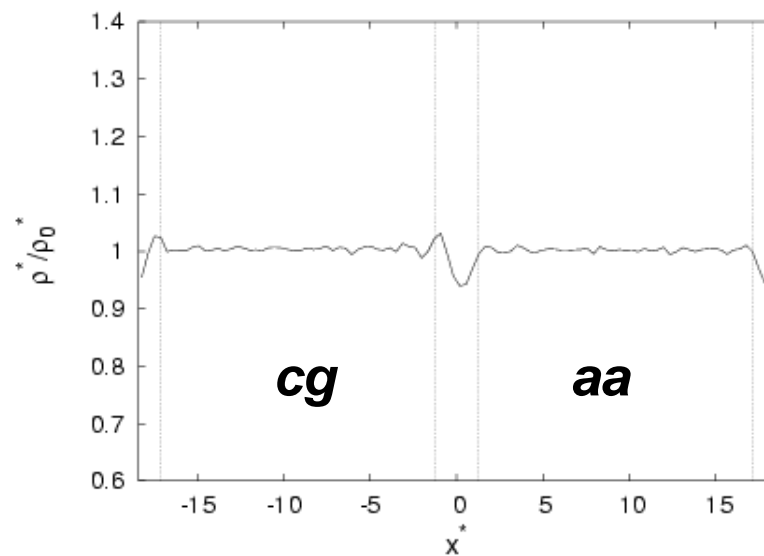
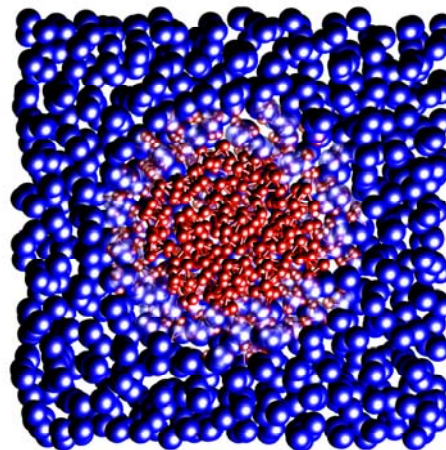
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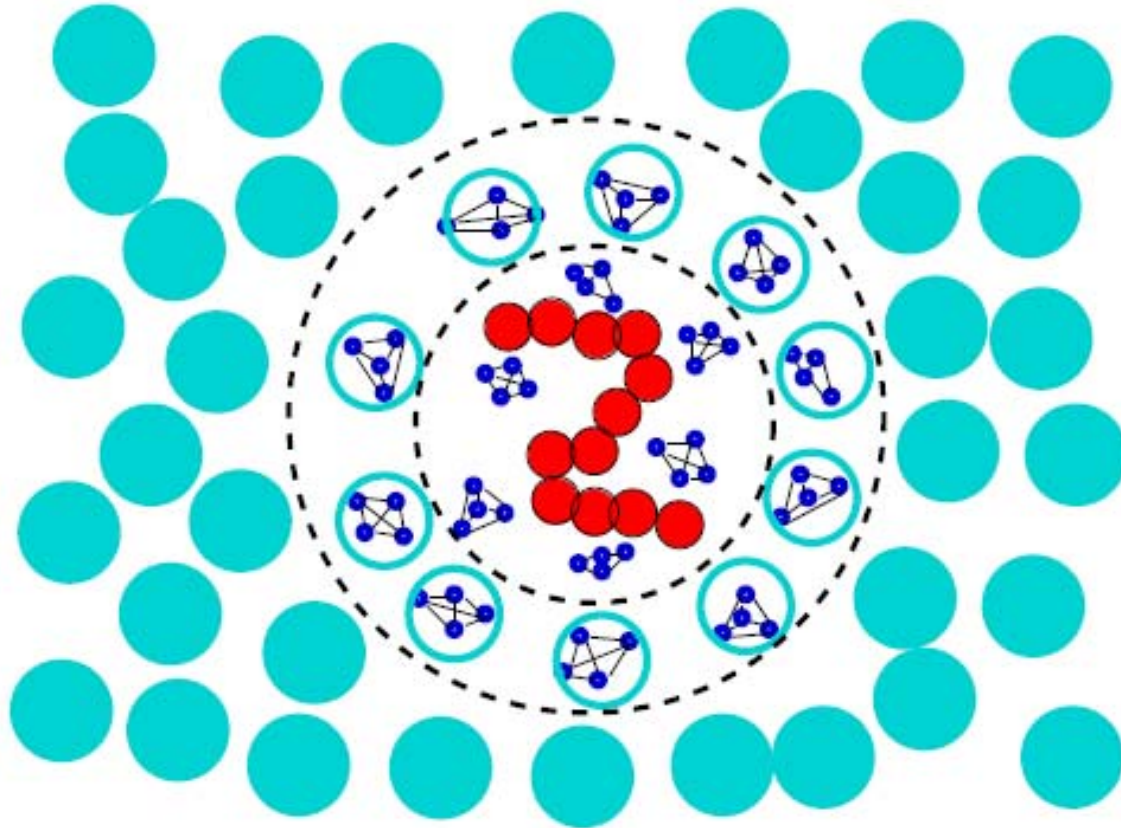
Particle Exchange



Particle Numbers, Density



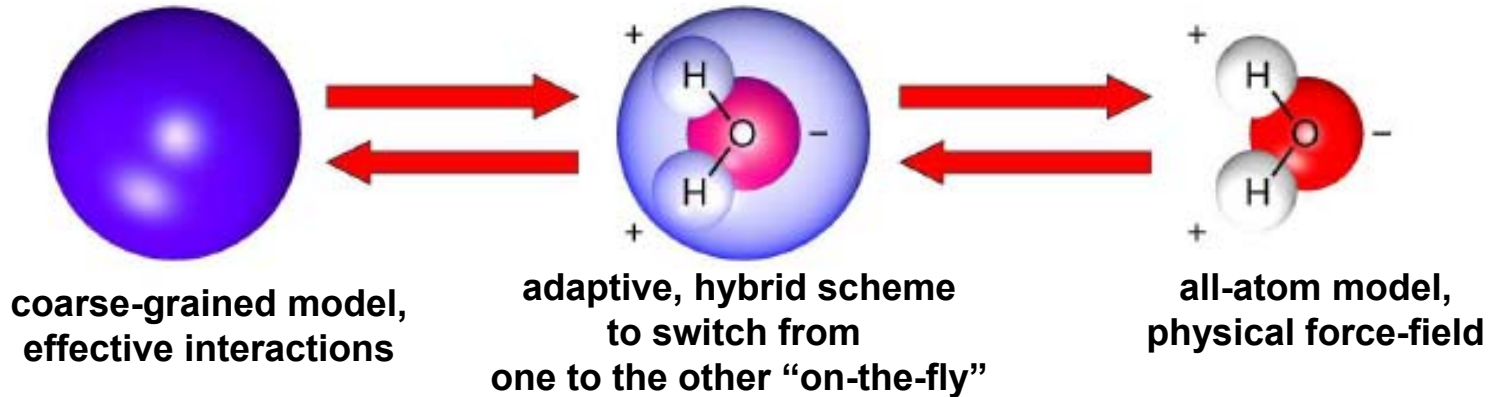
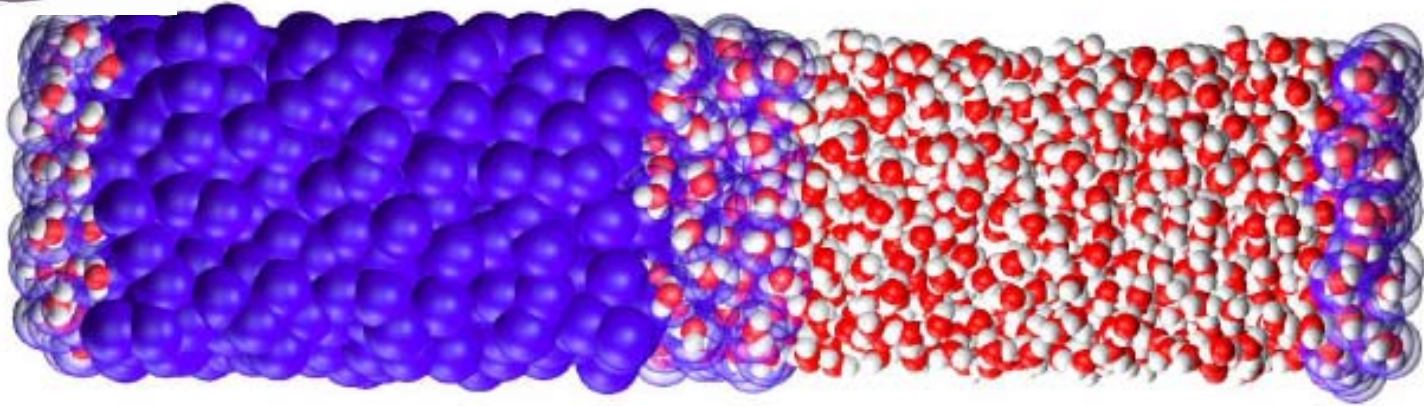
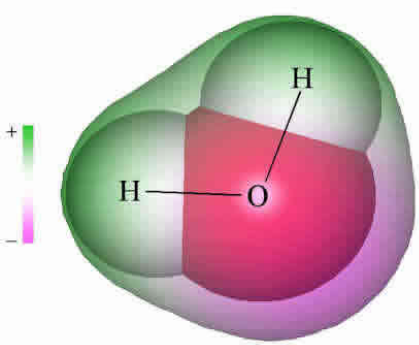
1st Application: Chain in solvent



Explicit resolution regime moves with the polymer

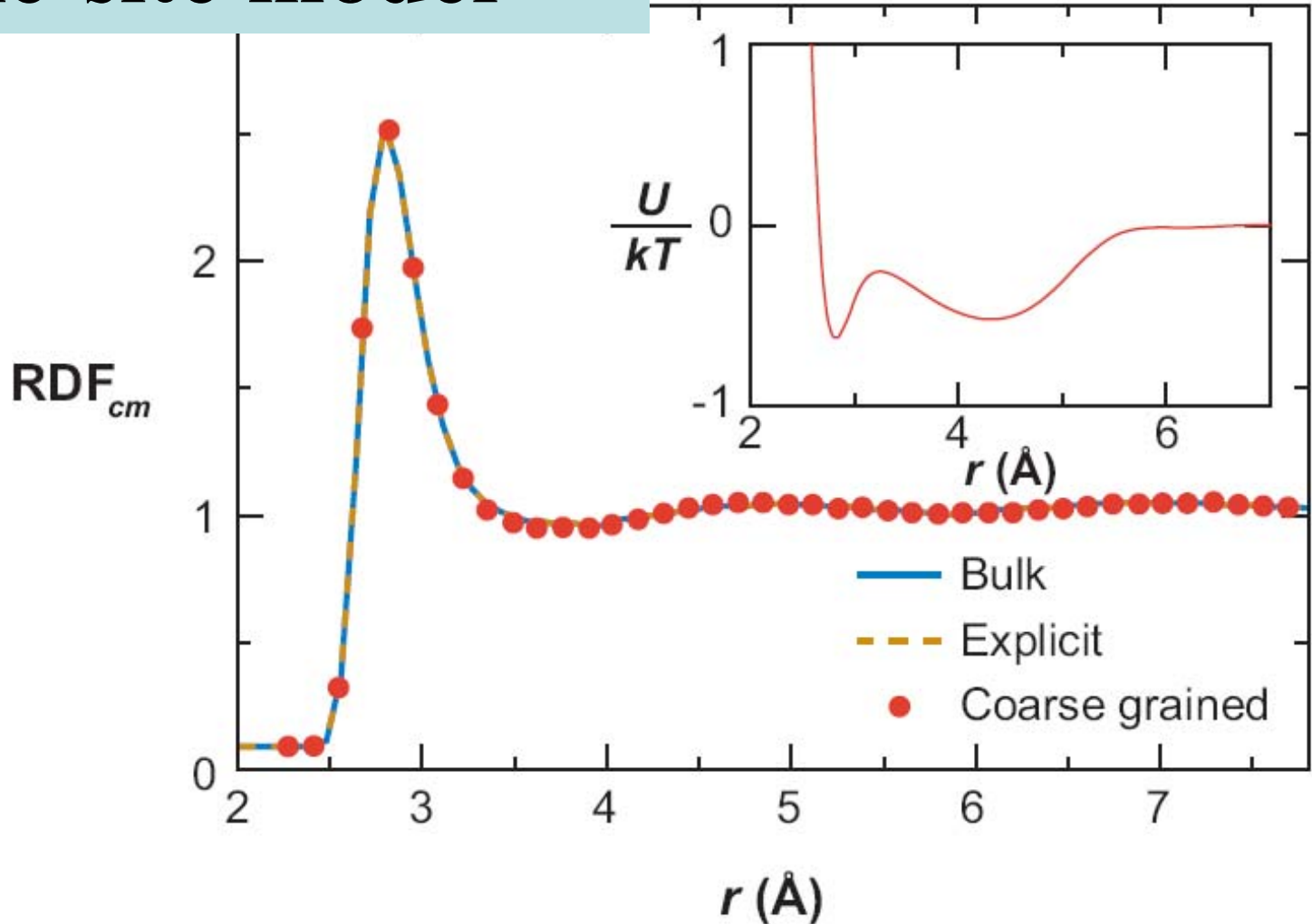
M. Praprotnik, L. Delle Site, KK, JCP (2007)

2nd Application TIP3P Water



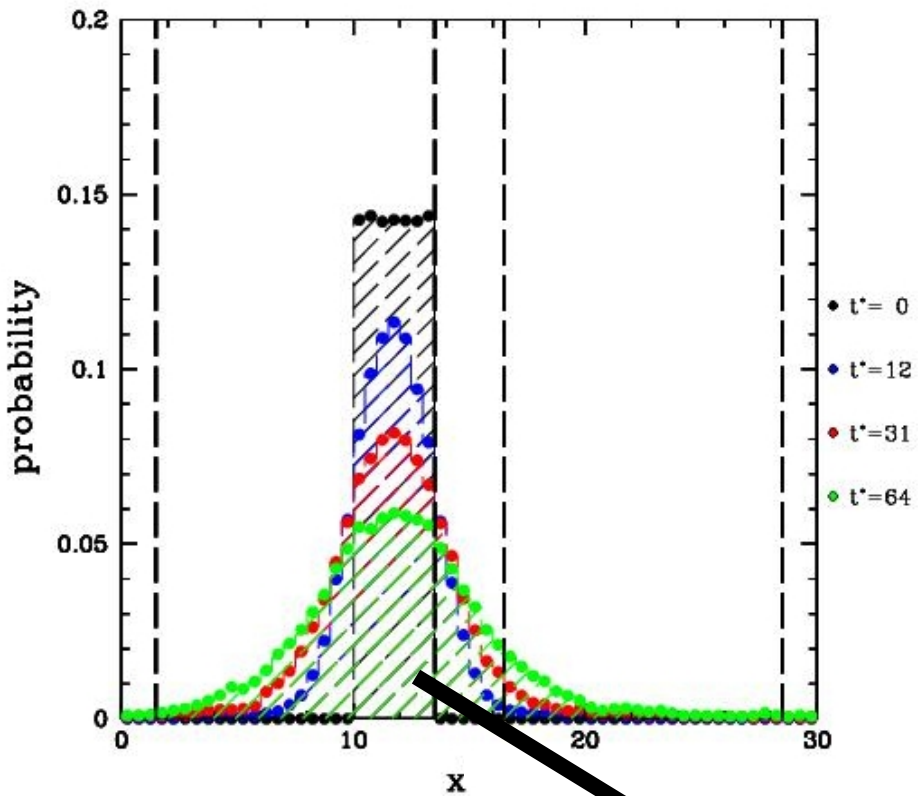
M. Praprotnik, S. Matysiak, L. Delle Site, K. Kremer, C. Clementi; J. Phys.: Condens. Matter; 19, 292201 (2007).

Single-site model

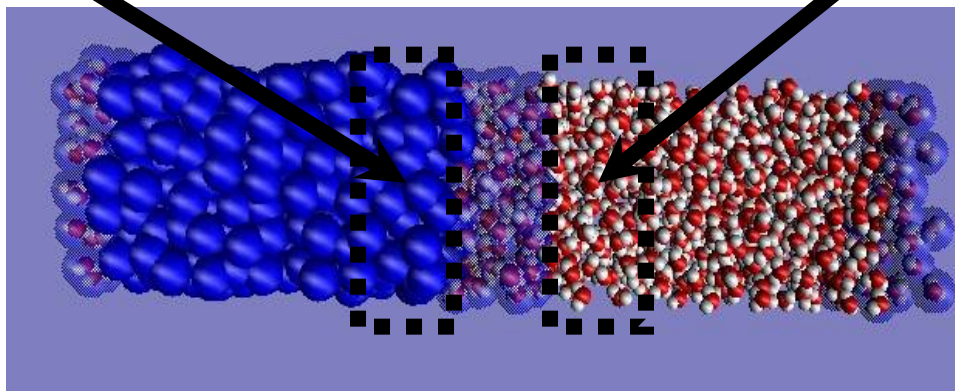
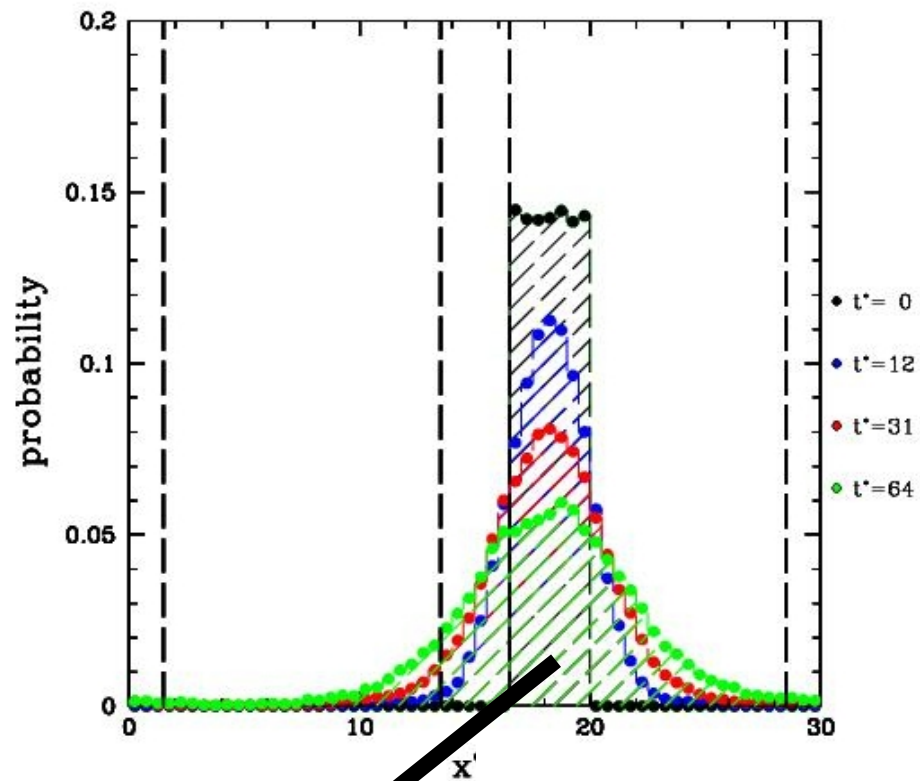


Pressure, temperature are also in excellent agreement, 4 nearest neighbors in first shell, tetrahedral order in 2nd shell for cg model almost completely lost

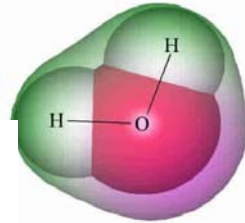
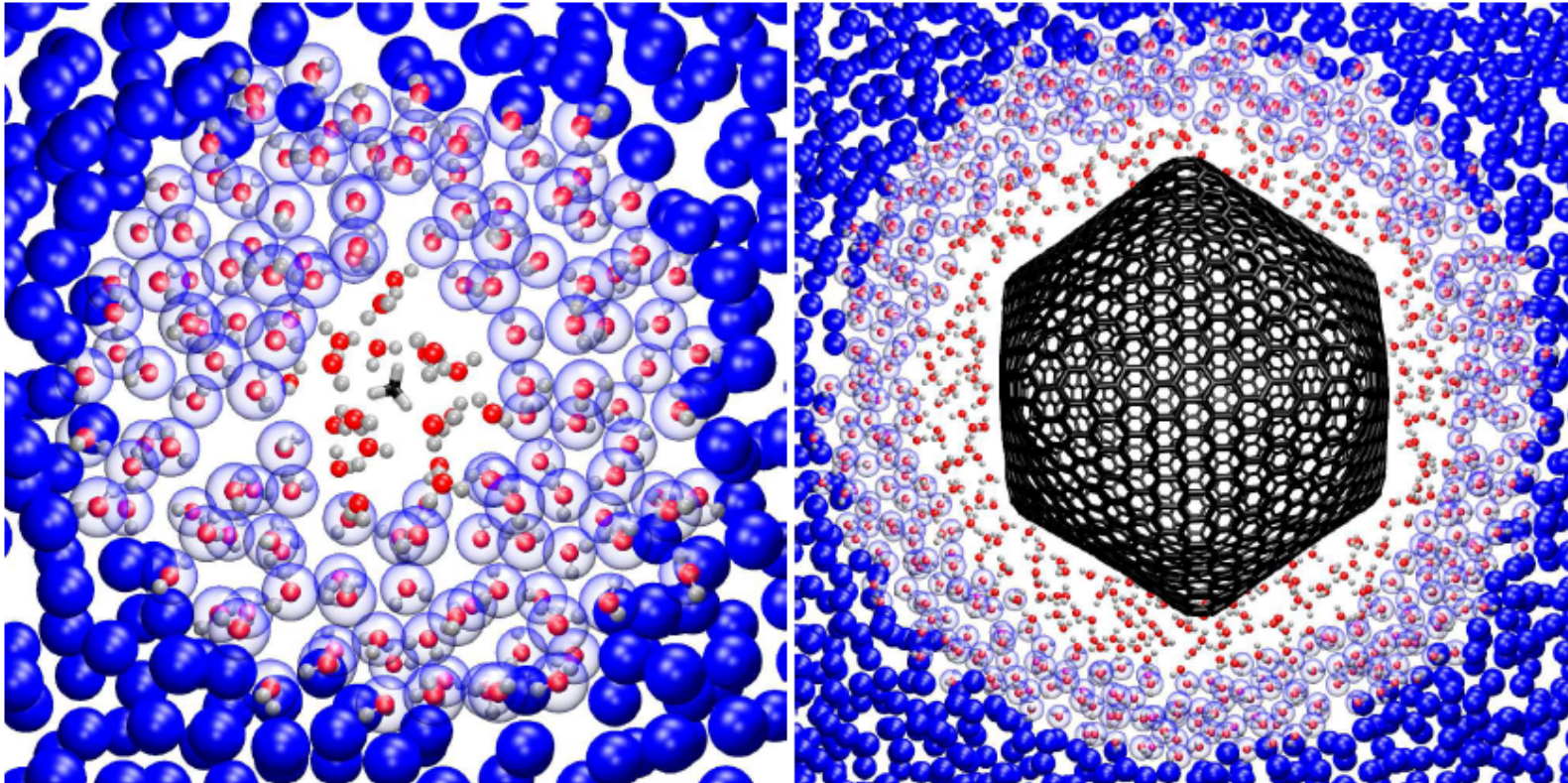
coarse grained hybrid explicit



coarse grained hybrid explicit



3rd Application Hydrophobic Solutes

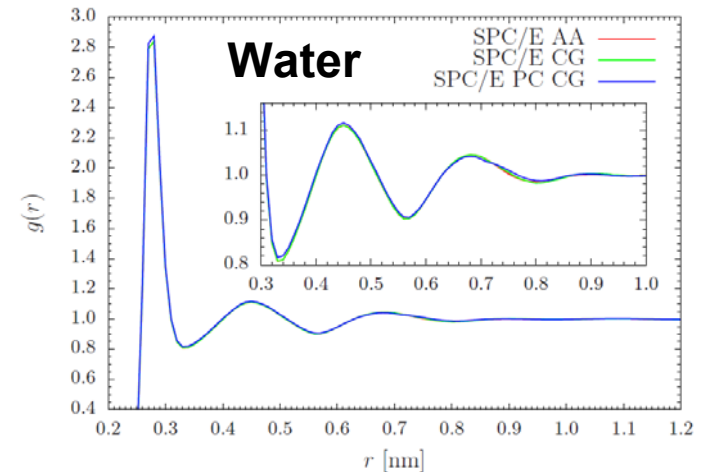
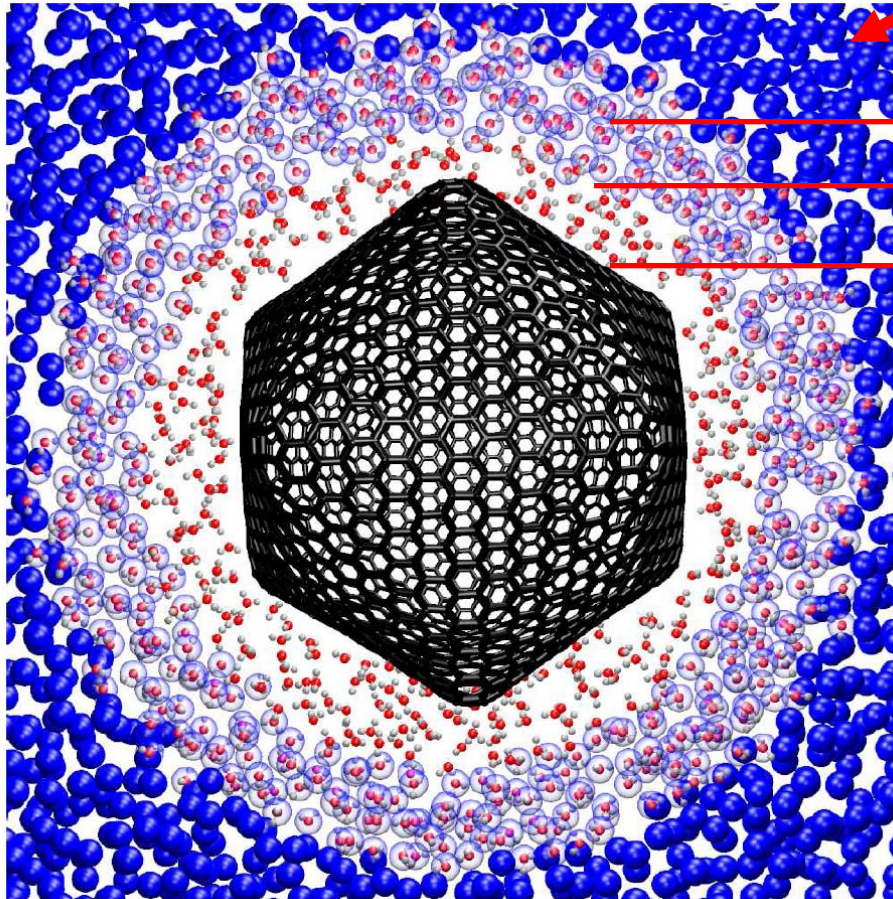


Hydrophobic Solutes: Surface vs Bulk

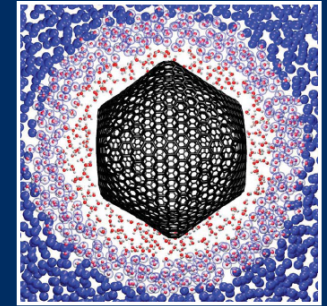
CG regime

Transition layer

All atom layer, d_{ex}



cg water reproduces $g(r)$
but NOT tetrahedral packing!



Hydrophobic Solutes

C₆₀



C₂₁₆₀

Influence of bulk H-bond structure on surface layer

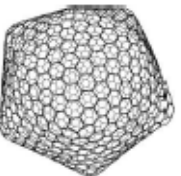
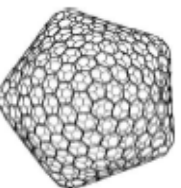
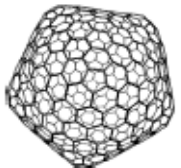
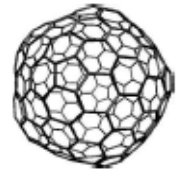
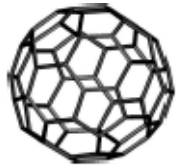
two surface potentials

- standard (weak) Lennard Jones

($\epsilon_{CO} \approx 0.2 k_B T$, $\sigma_{CO} \approx 0.34 \text{ nm}$)

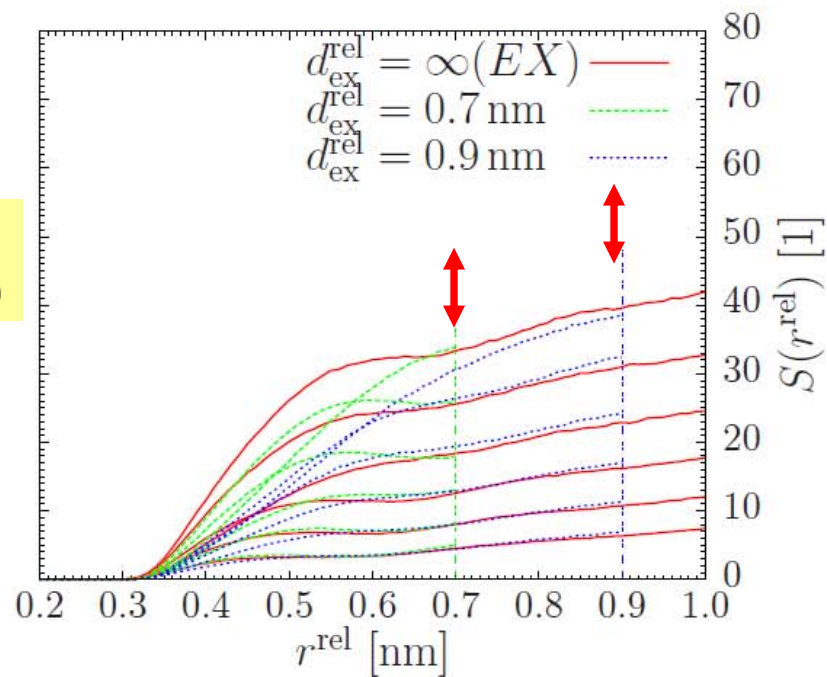
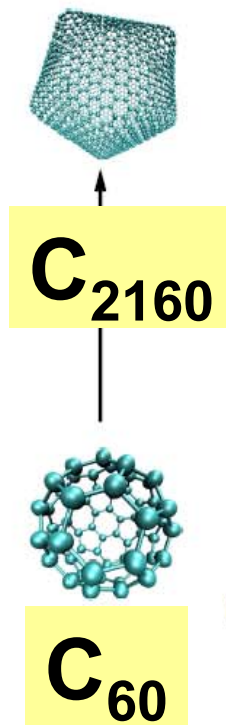
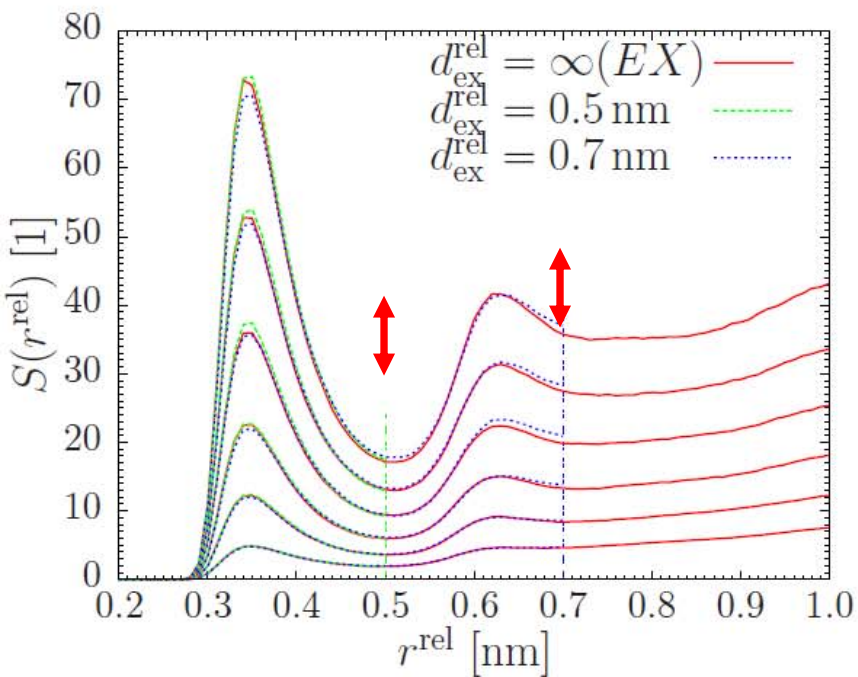
- purely repulsive (r^{-12})

variable width of explicit layer



of Water Molecules around Solute, variable all atom water layer

$d_{\text{ex}} (\approx 1^{\text{st}}, 2^{\text{nd}} \text{ shell}, \infty)$



LJ interaction

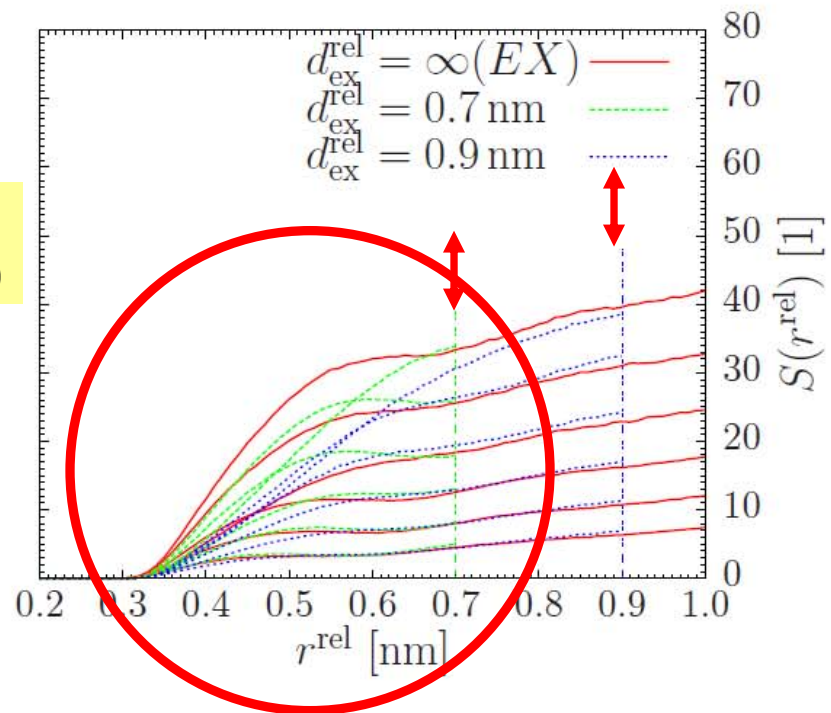
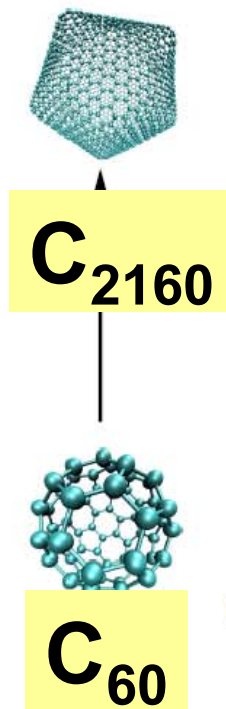
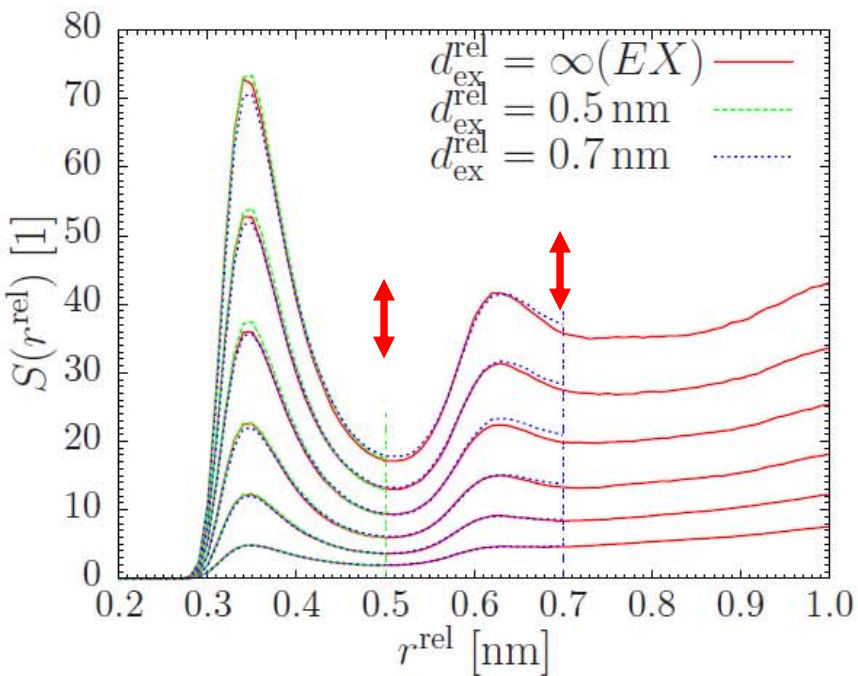
dominated by surface
Interaction

Repulsive

of waters close to surface
strongly depleted

of Water Molecules around Solute, variable all atom water layer

$d_{\text{ex}} (\approx 1^{\text{st}}, 2^{\text{nd}} \text{ shell}, \infty)$



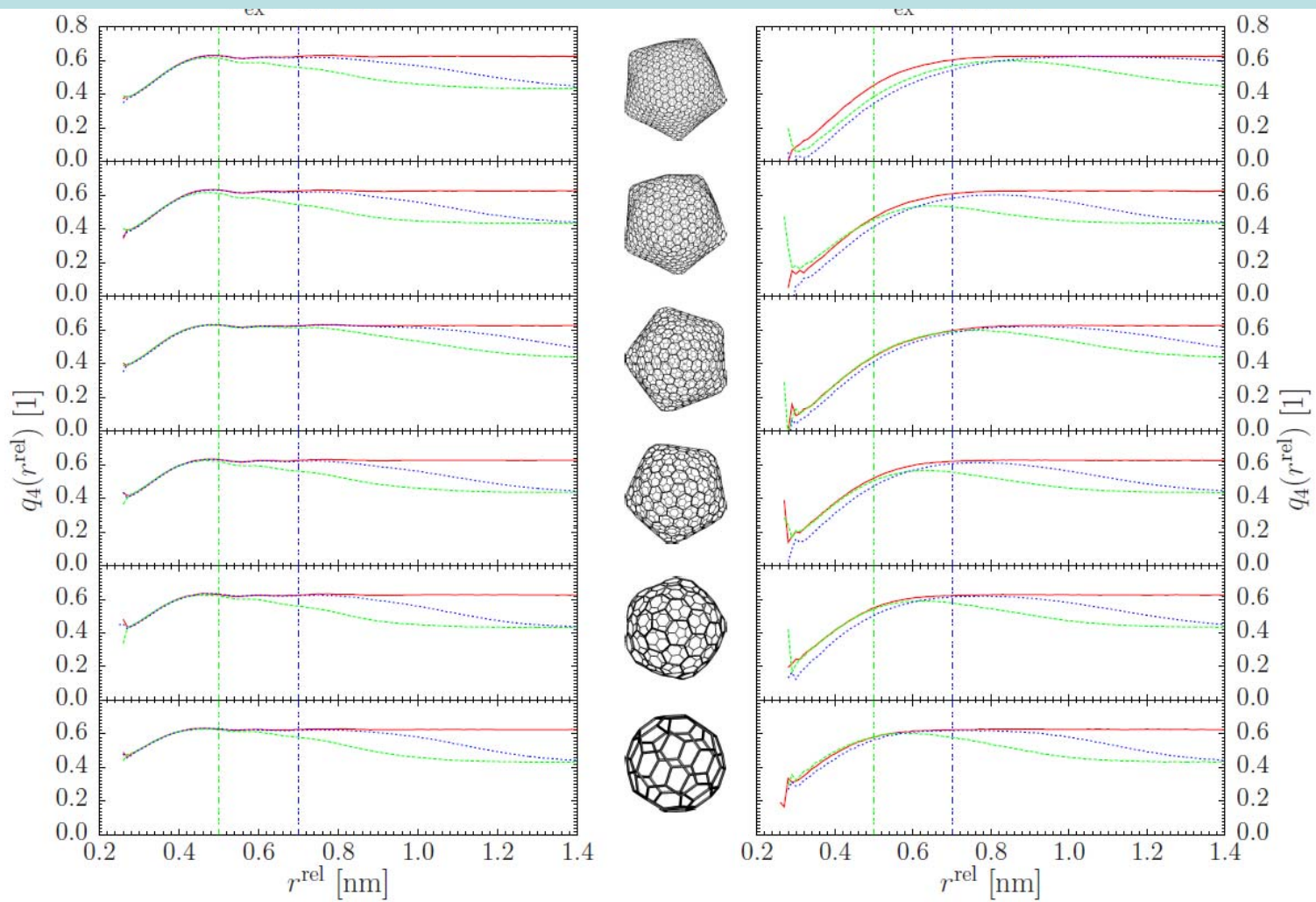
LJ interaction

dominated by surface
Interaction

Repulsive

of waters close to surface
strongly depleted

Tetrahedral Order



LJ

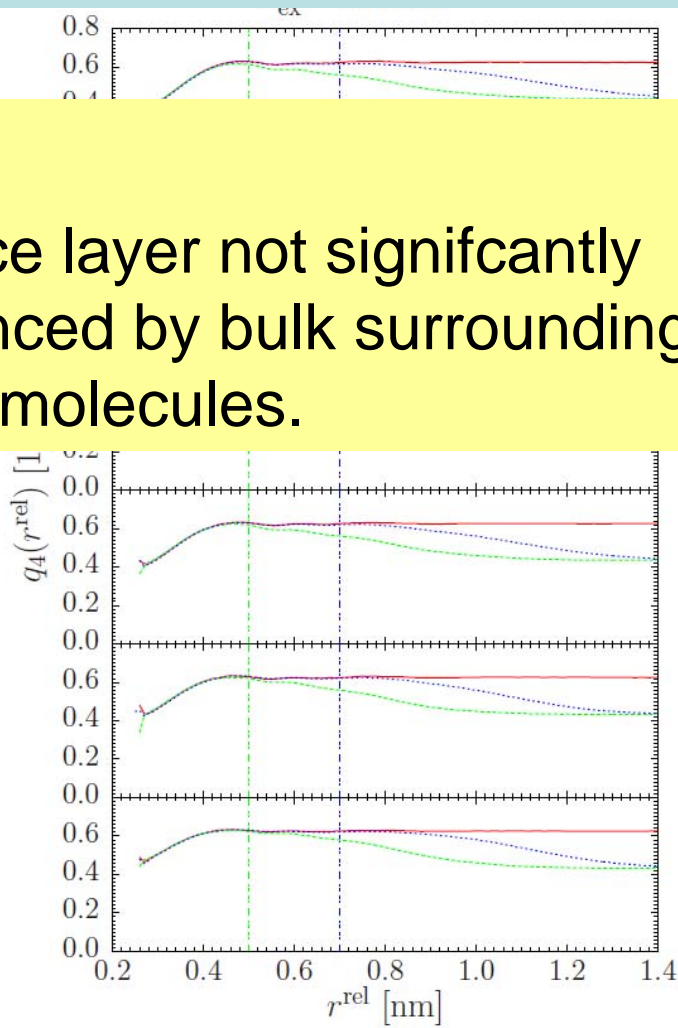
$$q_4 = 1 - \frac{3}{8} \sum_{i < j} \left[\cos(\theta_{ij}) - \frac{1}{3} \right]^2,$$

Repulsive

Tetrahedral Order

LJ:

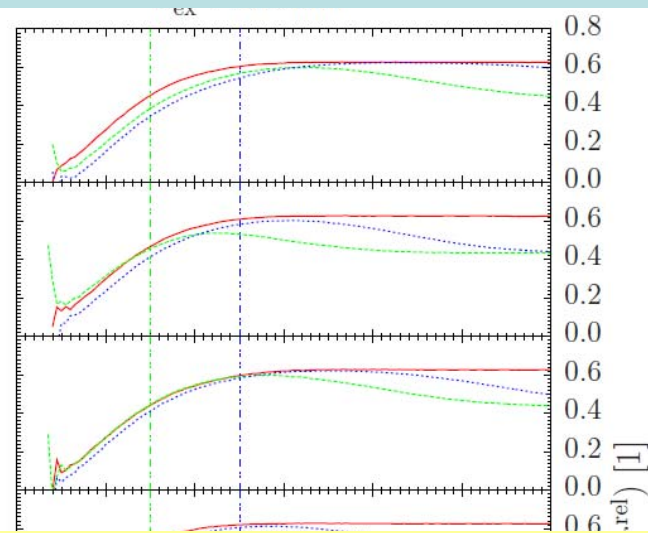
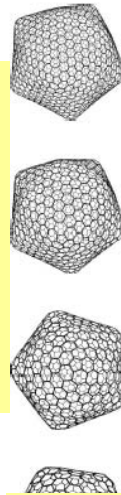
Surface layer not significantly influenced by bulk surrounding for all molecules.



LJ

$$q_4 = 1 - \frac{3}{8} \sum_{i < j} \left[\cos(\theta_{ij}) - \frac{1}{3} \right]^2,$$

Repulsive



Repulsive:

Density buildup needs structural support from bulk, order parameter seems independent of density (Compensation of effects?).

Transition Regime, Generalizations

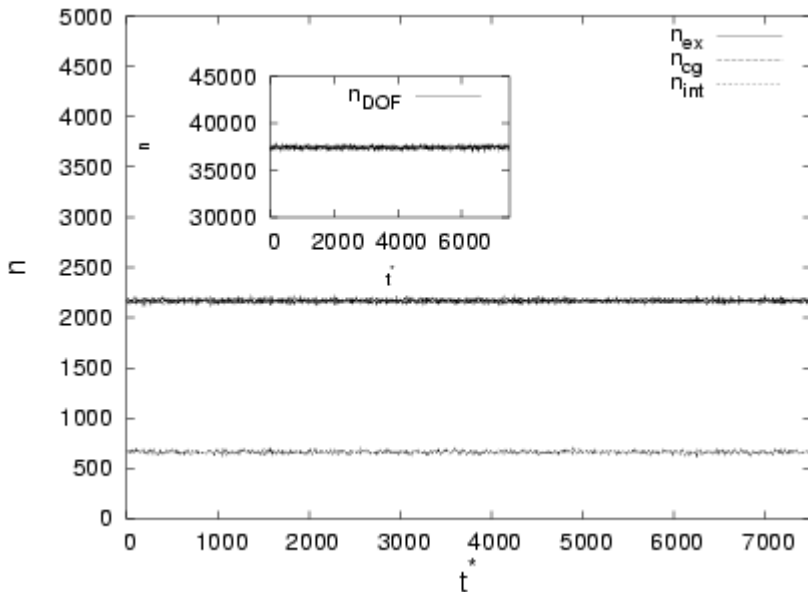
Density wiggles in transition regime

=> thermodynamic force to level off pressure

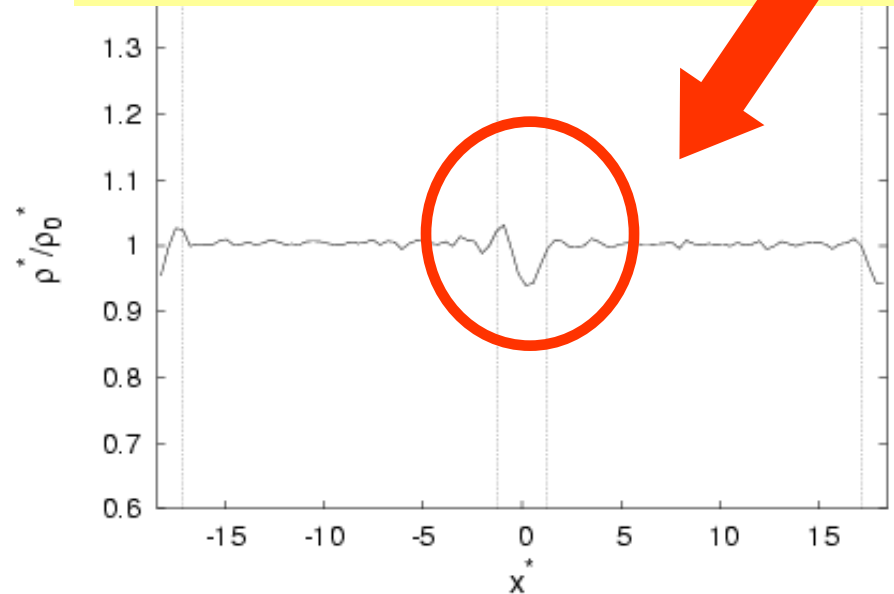
Generalization

=> “Open System” MD

Particle Numbers, Density

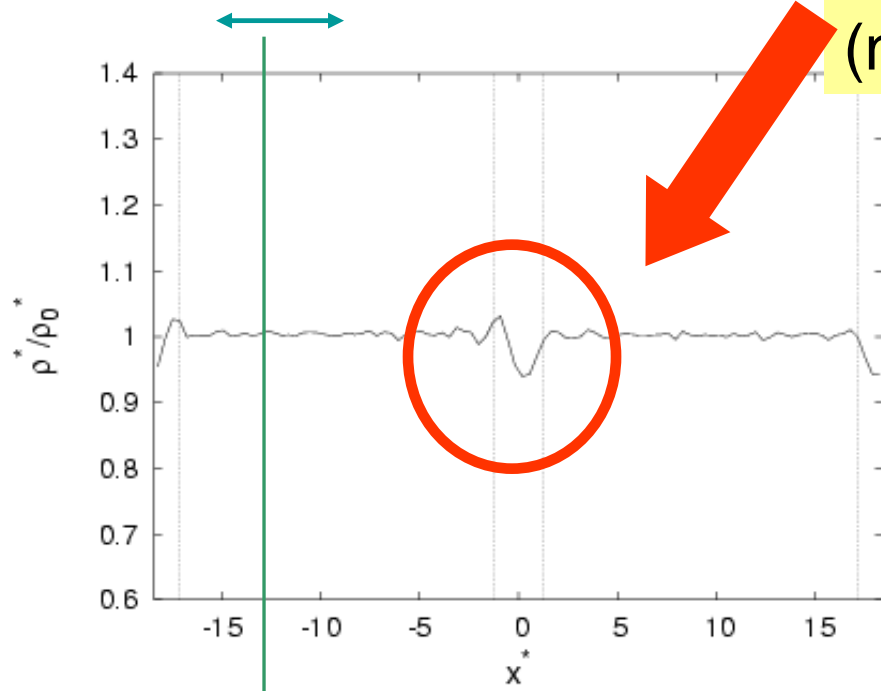


Equation of state in transition Regime not the same!



Pressure

Equation of state in transition regime not the same!
(not surprising)



No potential energy function in whole system,
but
well defined forces and thus
well defined pressures

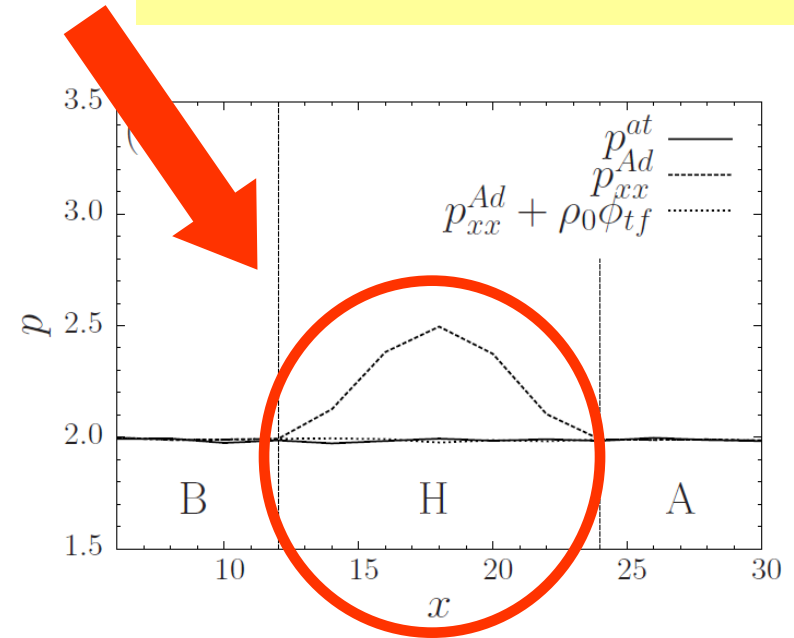
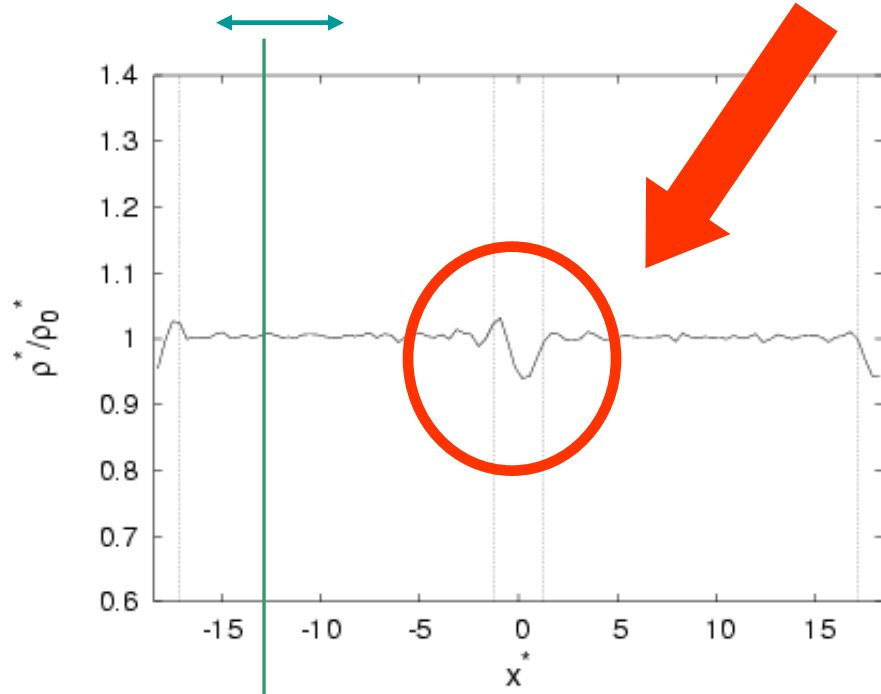
Calculate pressure in a plane $\perp x$

(Todd, Evans, Davies)

$$\bar{p}_{\beta\alpha}(\alpha) = \frac{1}{2A_{\alpha}\Delta\alpha} \left\langle \sum_{\alpha-\Delta\alpha \leq \alpha_i \leq \alpha+\Delta\alpha} m_i v_{i\beta} v_{i\beta} \right\rangle + \frac{1}{2A_{\alpha}} \left\langle \sum_{i=1}^N F_{i\beta} \text{sgn}(\alpha_i - \alpha) \right\rangle$$

Pressure

If density fixed to constant value
 \Rightarrow Pressure bump in hybrid zone



Calculate pressure in a plane $\perp x$

(Todd, Evans, Davies)

$$\bar{p}_{\beta\alpha}(\alpha) = \frac{1}{2A_\alpha \Delta\alpha} \left\langle \sum_{\alpha - \Delta\alpha \leq \alpha_i \leq \alpha + \Delta\alpha} m_i v_{i\beta} v_{i\beta} \right\rangle + \frac{1}{2A_\alpha} \left\langle \sum_{i=1}^N F_{i\beta} \text{sgn}(\alpha_i - \alpha) \right\rangle$$

Pressure

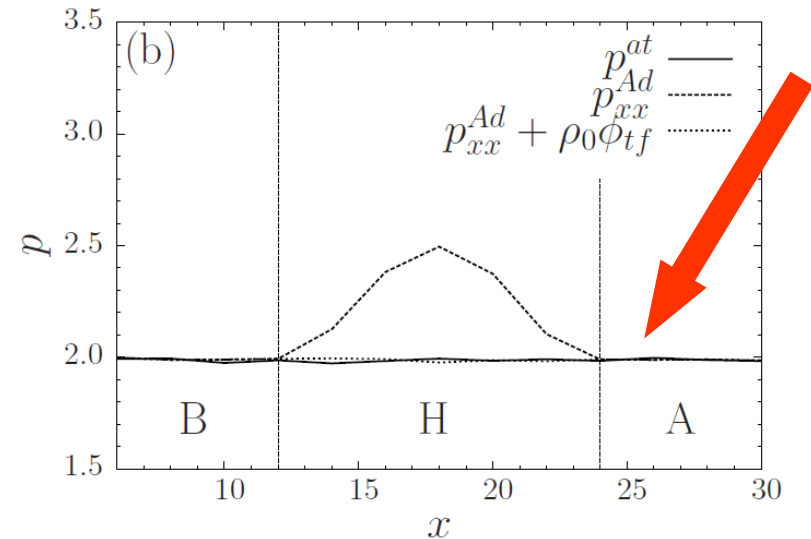
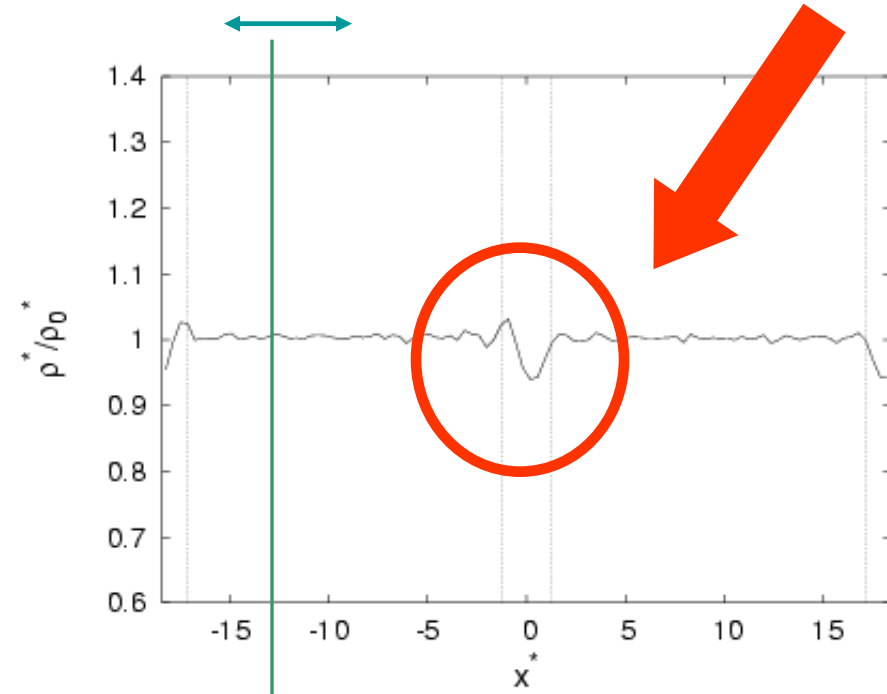
If density fixed to constant value

⇒ Pressure bump in hybrid zone

⇒ Thermodynamic force, iterate

$$f_{th} = \frac{1}{\rho_0} \nabla p_f$$

Well defined constant pressure ensemble



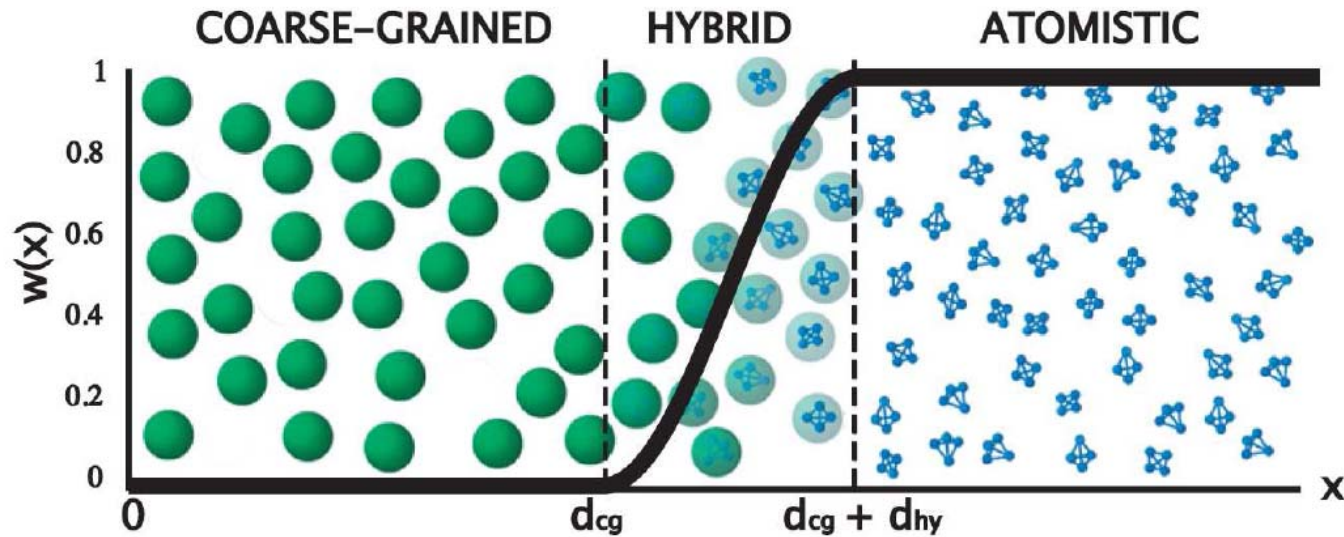
Calculate pressure in a plane $\perp x$

(Todd, Evans, Davies)

$$\bar{p}_{\beta\alpha}(\alpha) = \frac{1}{2A_\alpha \Delta\alpha} \left\langle \sum_{\alpha - \Delta\alpha \leq \alpha_i \leq \alpha + \Delta\alpha} m_i v_{i\beta} v_{i\beta} \right\rangle + \frac{1}{2A_\alpha} \left\langle \sum_{i=1}^N F_{i\beta} \text{sgn}(\alpha_i - \alpha) \right\rangle$$

Pressure based “Thermodynamic Force”

(alternative route via chemical potential, S. Poblete, M. Praprotnik, KK, L. Delle Site, JCP, 132, 114101 (2010))



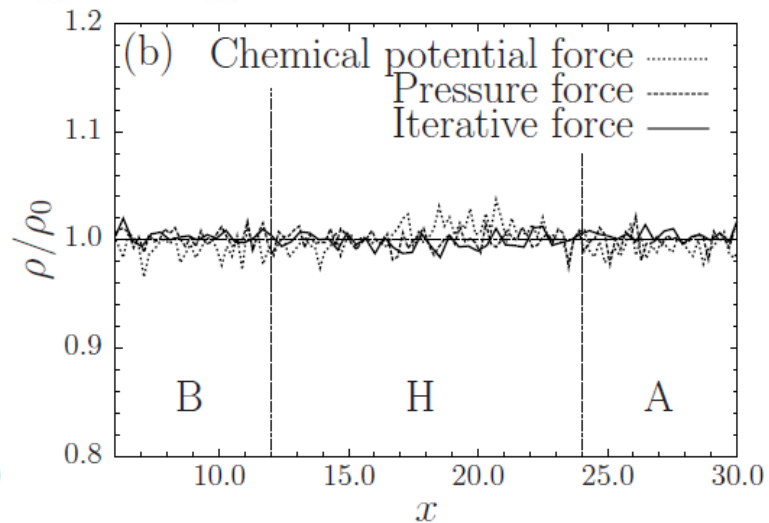
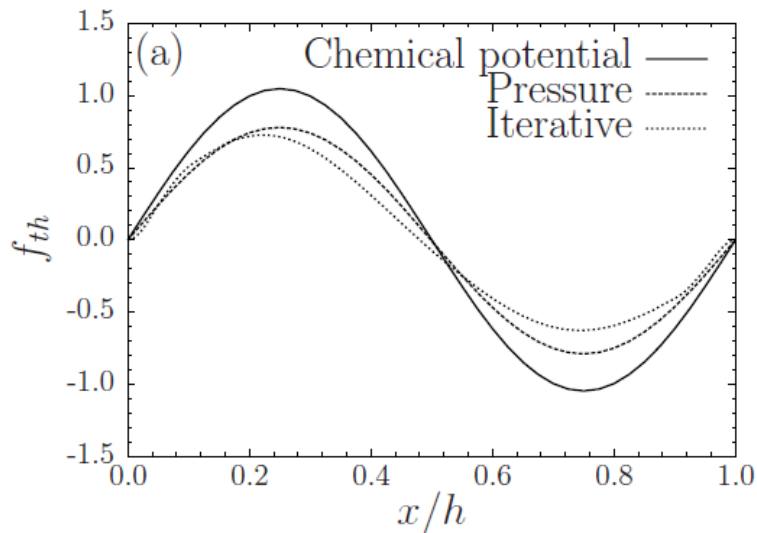
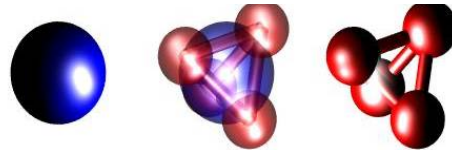
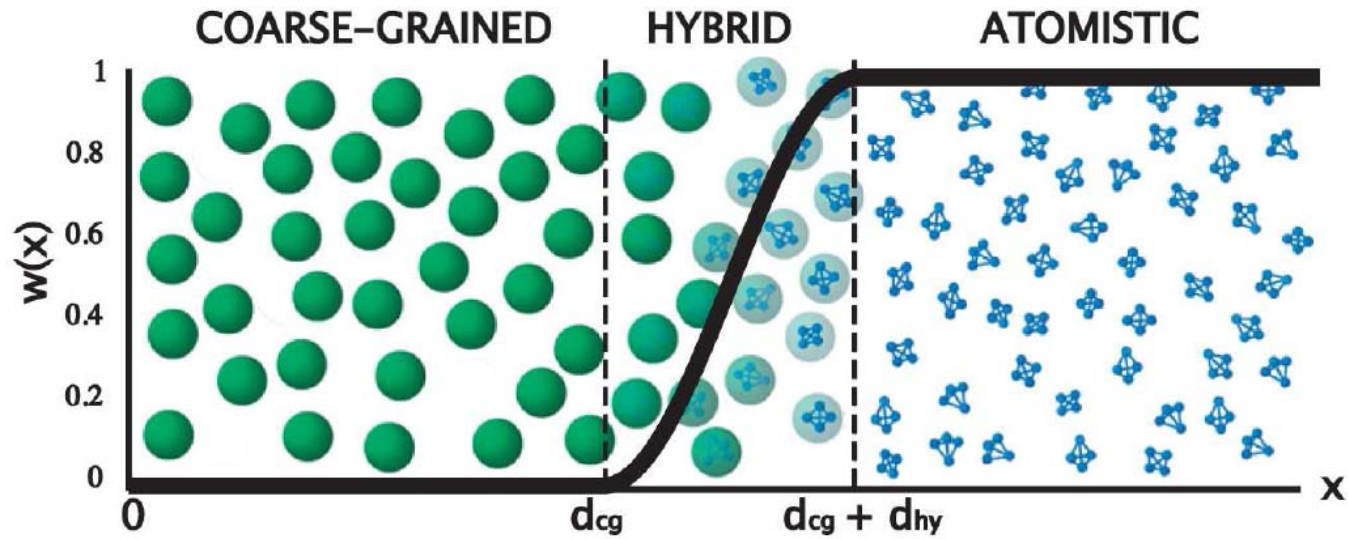
$$p(\mathbf{r}, \rho(\mathbf{r} = \rho_0)) \approx p_{ad} + \frac{1}{\rho_0 \kappa_T(\mathbf{r})} (\rho_0 - \rho_{ad}(\mathbf{r}))$$

$$\mathbf{f}_{th} = -\frac{1}{\rho_0} \nabla (p_{at} - p(\mathbf{r}))$$

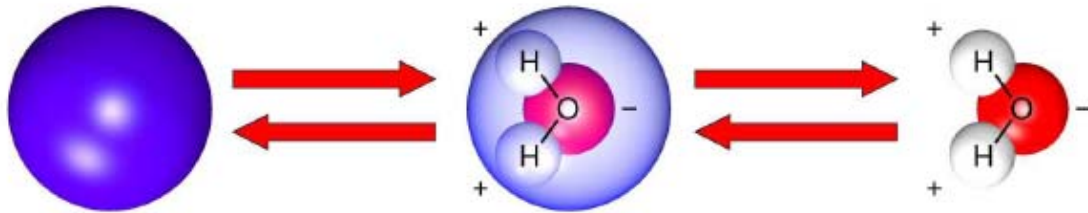
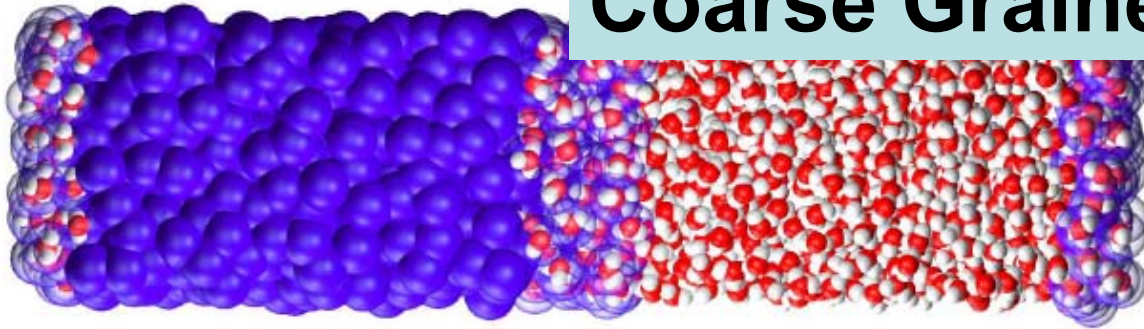
$$\mathbf{f}_{th}^{i+1}(\mathbf{r}) = \mathbf{f}_{th}^i(\mathbf{r}) - \frac{1}{\rho_0^2 \kappa_T^{at}} \nabla \rho_i(\mathbf{r})$$

S. Poblete, G. Ciccotti, I. Delle Site, KK, in preparation

Pressure based Thermodynamic Force



Coarse Grained Water: SPC/E



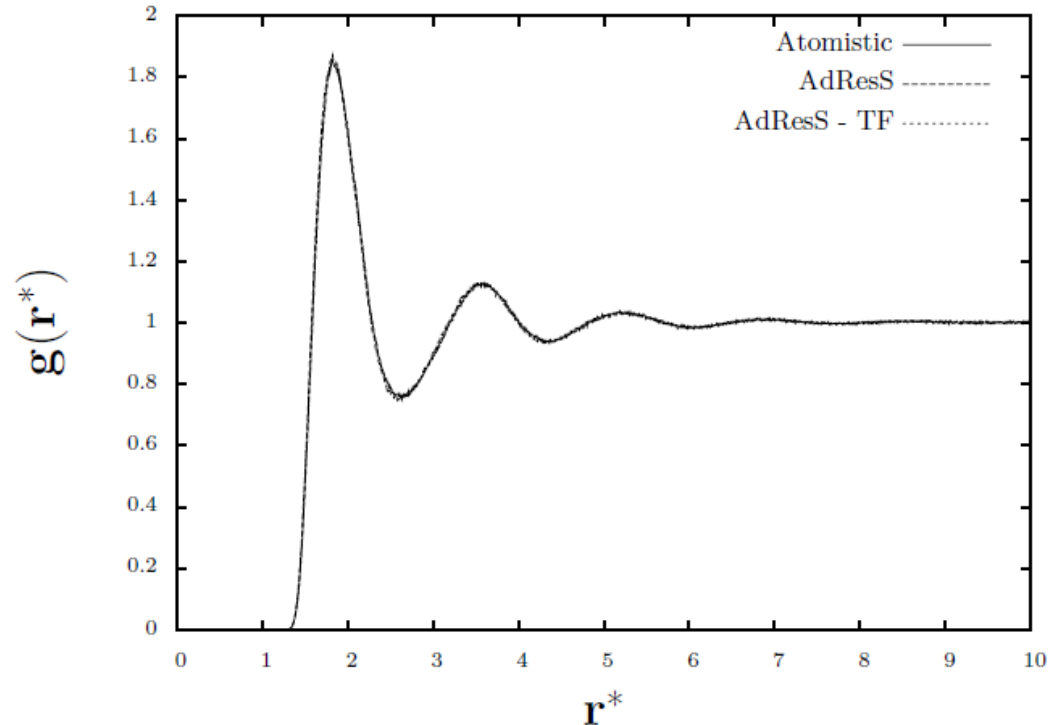
Structure based
Coarse Graining:

Perfect match of $g(r)$
all atom – coarse grained

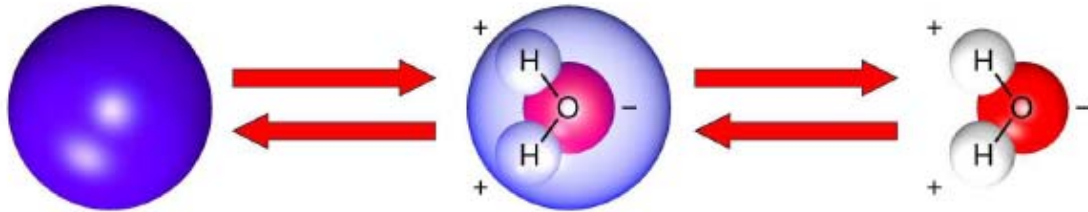
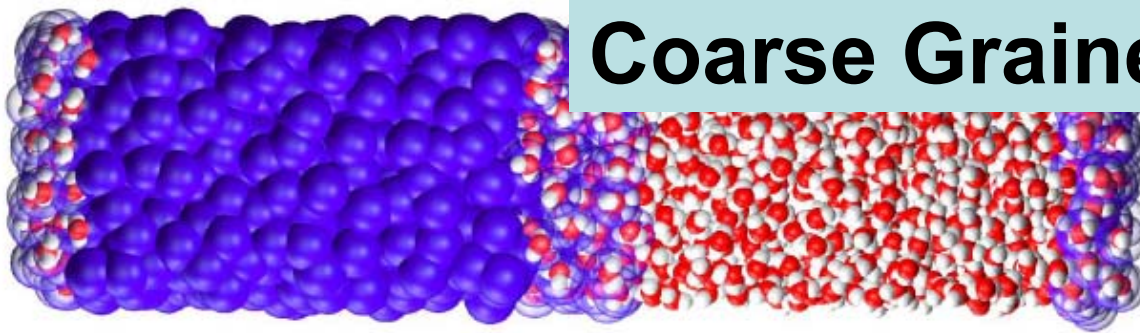
$$\kappa_{\text{atomistic}} = \kappa_{\text{cg}}$$

BUT

$$\rho_{\text{cg}} = 6200\rho_{\text{atomistic}}$$



Coarse Grained Water: SPC/E



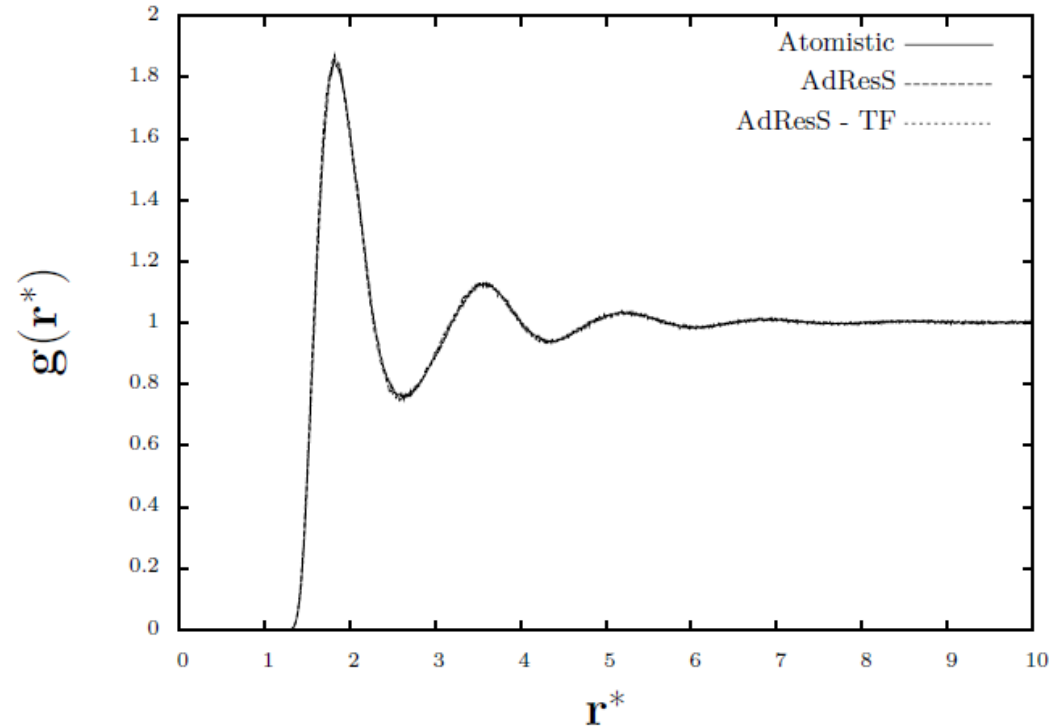
Structure based
Coarse Graining:

Perfect match of $g(r)$
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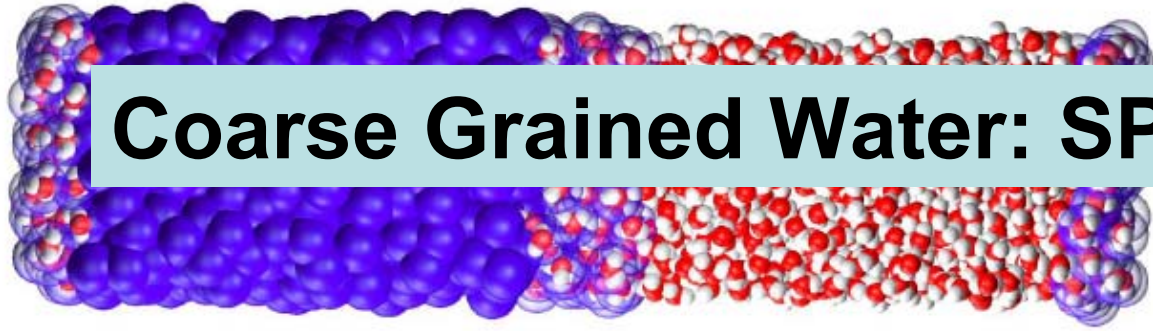
$$K_{\text{atomistic}} = K_{\text{cg}}$$

BUT

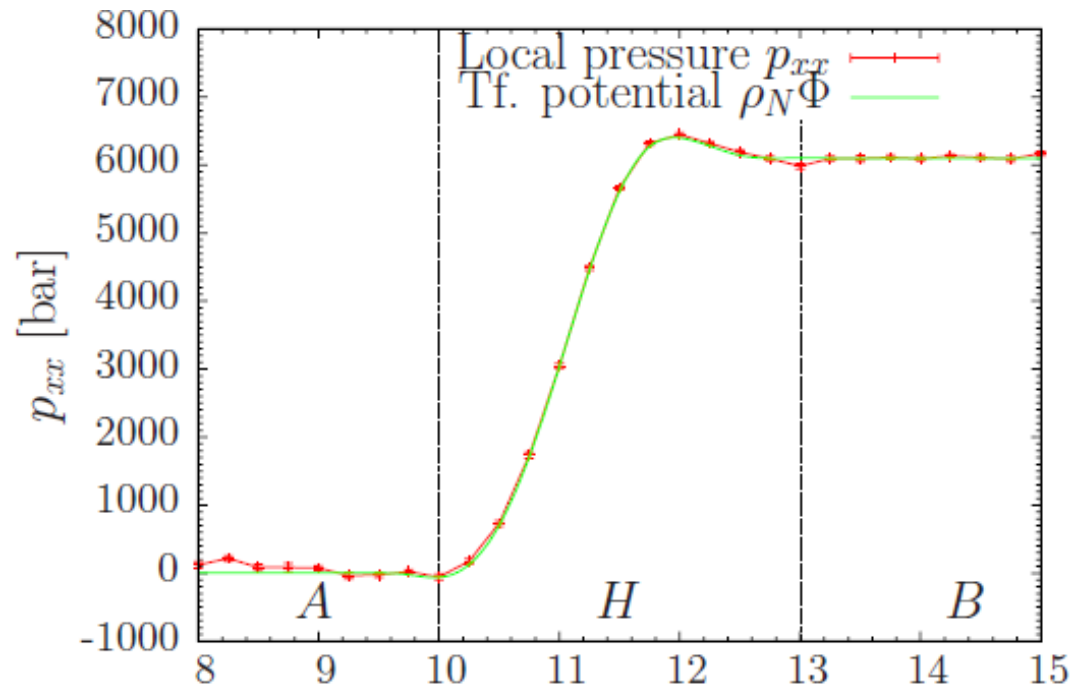
$$p_{\text{cg}} = 6200 p_{\text{atomistic}}$$



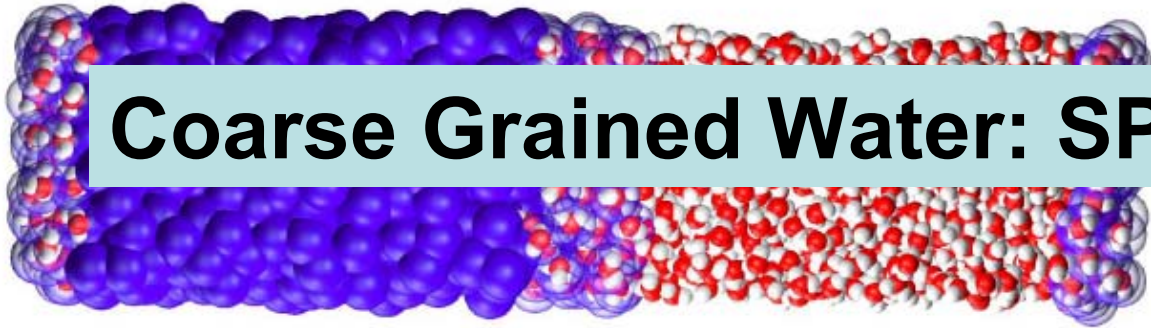
Coarse Grained Water: SPC/E



**Structure based Coarse Graining:
apply pressure based thermodynamic
correction force**

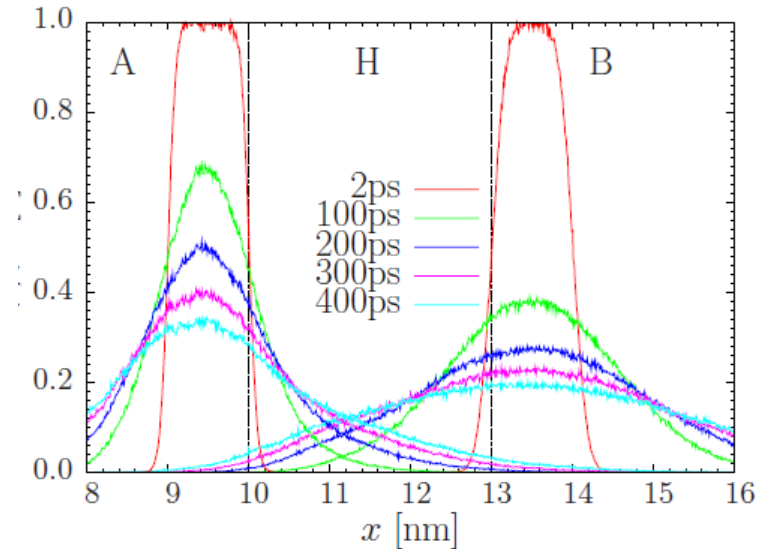
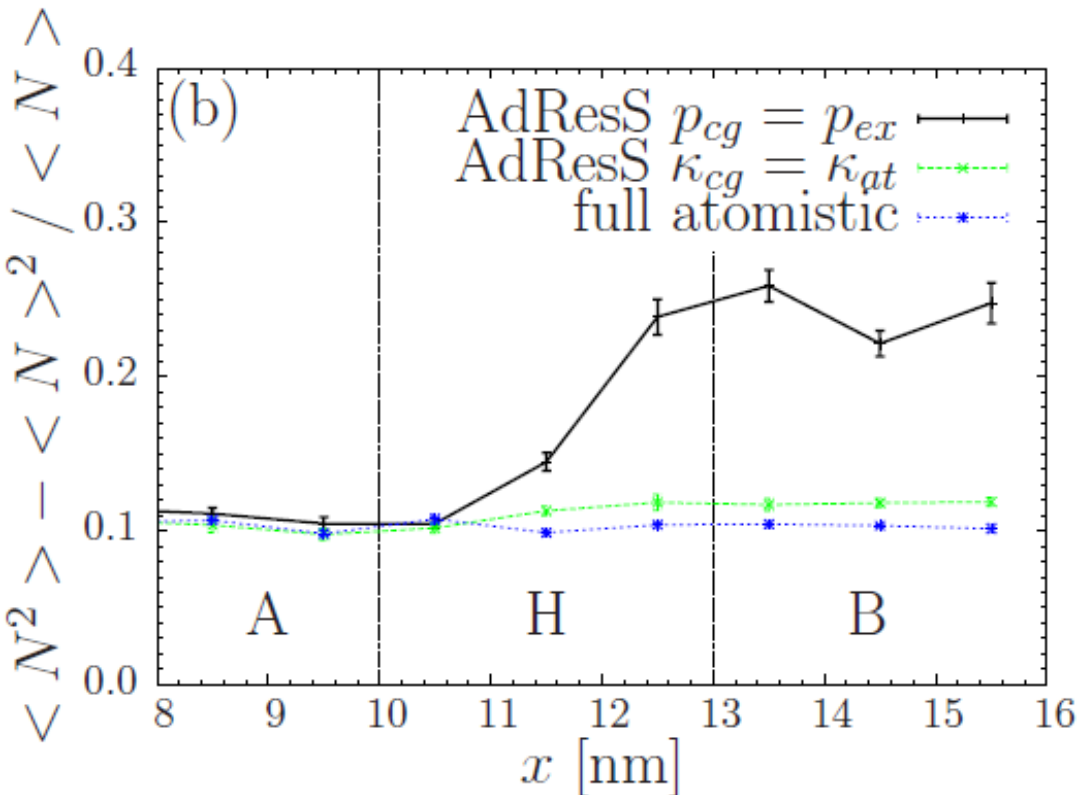


$$\bar{p}_{\beta\alpha}(\alpha) = \frac{1}{2A_\alpha\Delta\alpha} \left\langle \sum_{\alpha-\Delta\alpha \leq \alpha_i \leq \alpha+\Delta\alpha} m_i v_{i\beta} v_{i\beta} \right\rangle + \frac{1}{2A_\alpha} \left\langle \sum_{i=1}^N F_{i\beta} \text{sgn}(\alpha_i - \alpha) \right\rangle$$



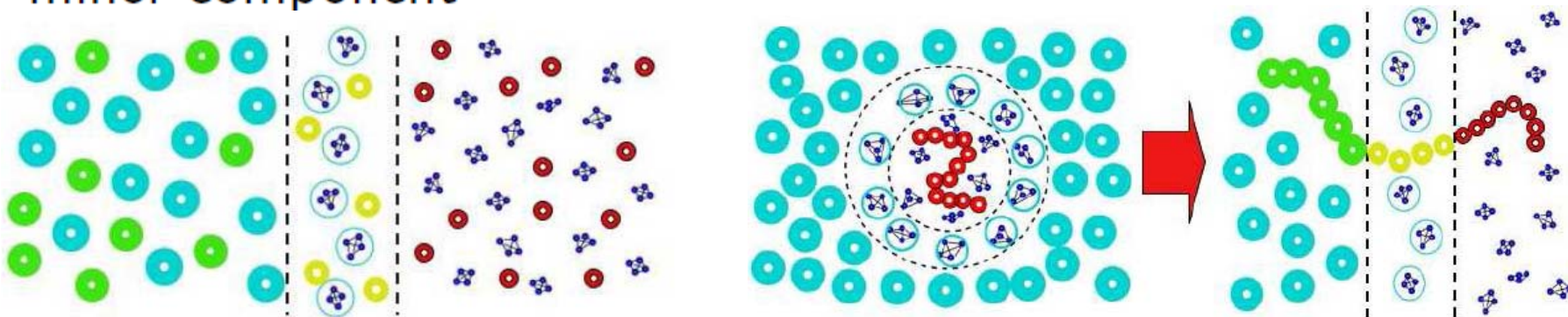
Coarse Grained Water: SPC/E

**Structure based Coarse Graining:
apply pressure based thermodynamic
correction force**



Extensions : Mixtures...

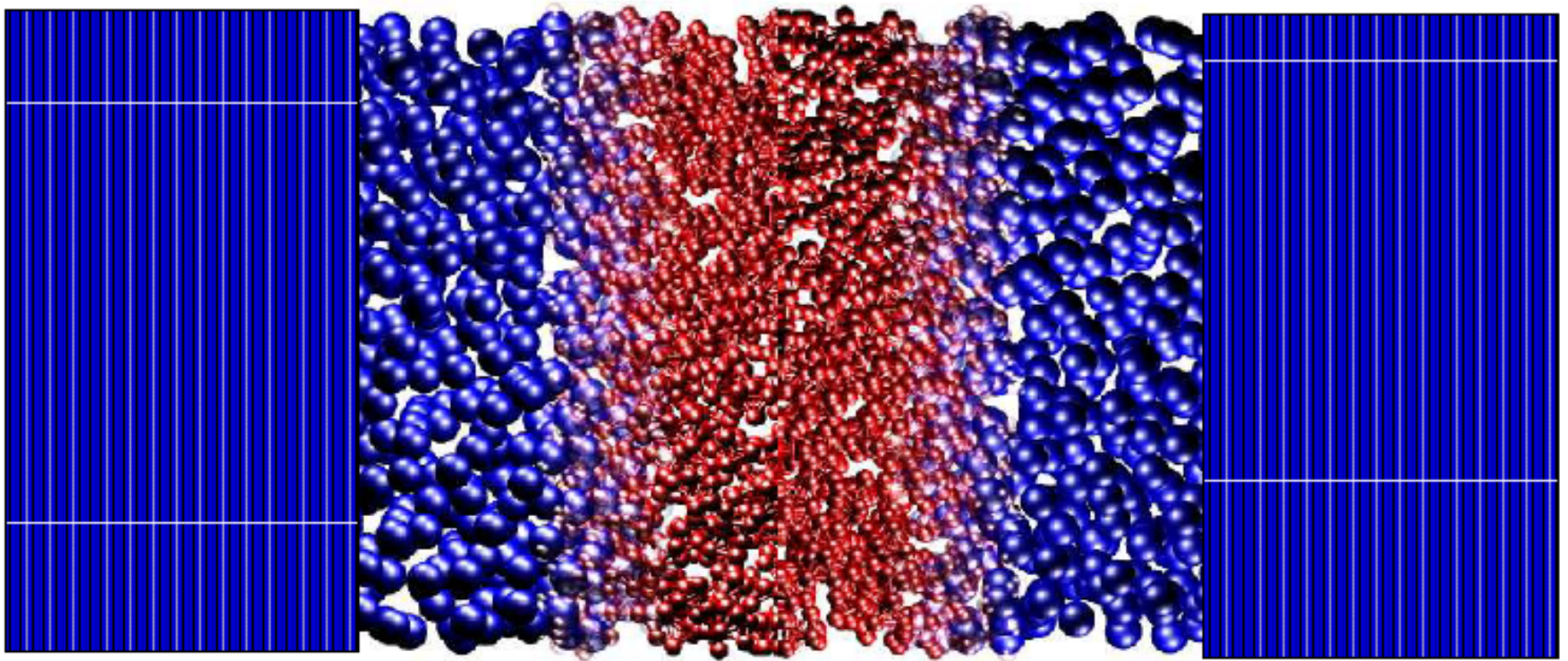
- (a) fundamental questions about the coarse-graining procedure: Structure reproduced, **but** how much of the thermodynamics?
- (b) Two species, two resolutions each: \rightarrow 4 different chemical potentials
- how to preserve equilibrium?
- Thermodynamic force proportional to the concentration of the minor component



Extensions AdResS:  **Continuum**
QM Description

Extension I:

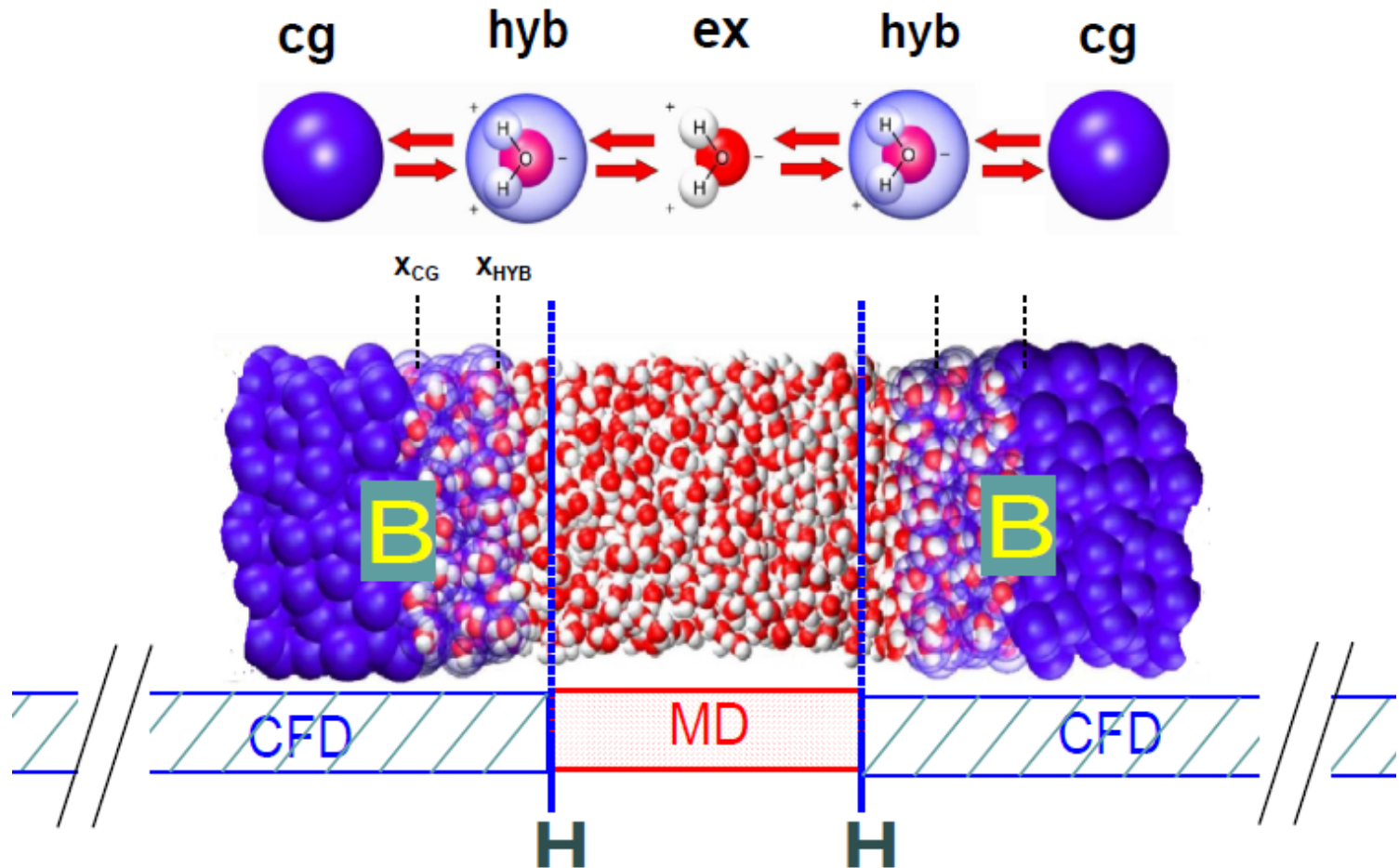
***Concurrent Triple-Scale Simulation of
Molecular Liquids***



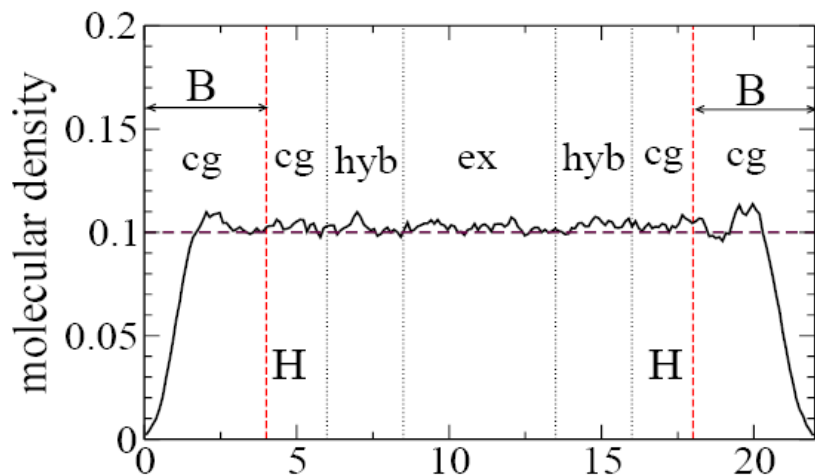
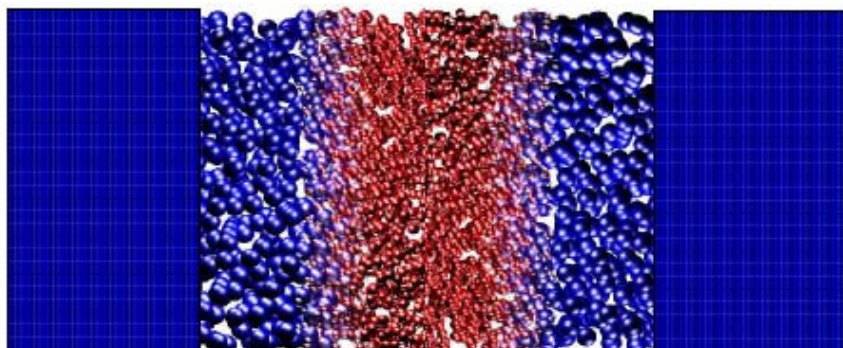
R. Delgado Buscalioni, KK, M. Praprotnik, JCP 128, 114110 (2008)

AdResS-HybridMD: Water

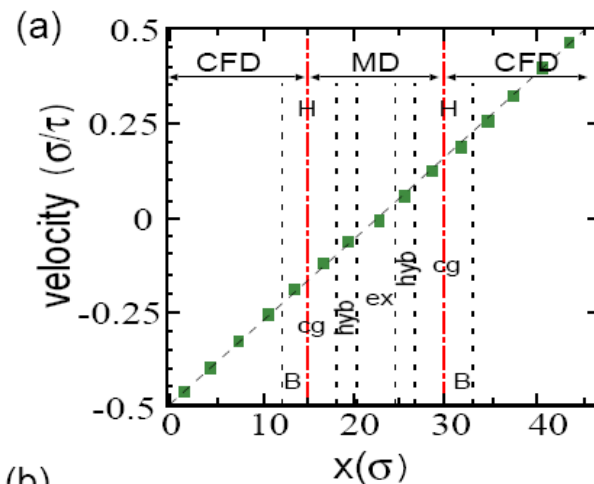
2nd Scheme



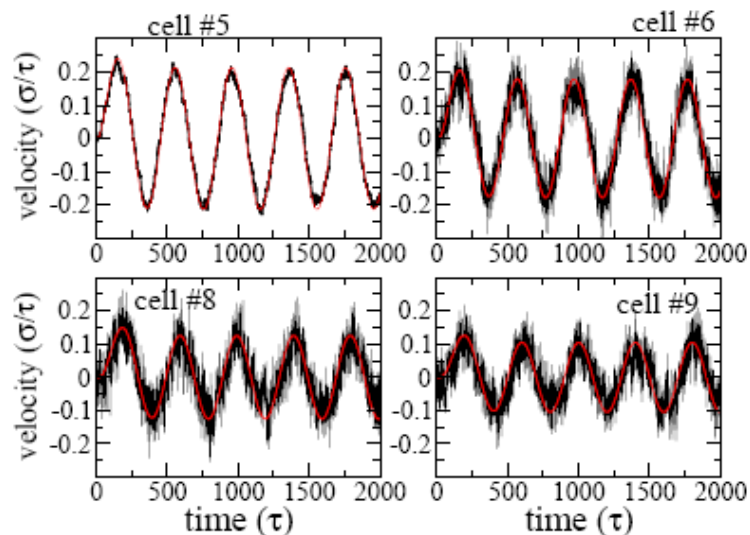
Concurrent Triple-Scale Simulation of Molecular Liquids



Simple shear



(b)



Oscillatory shear

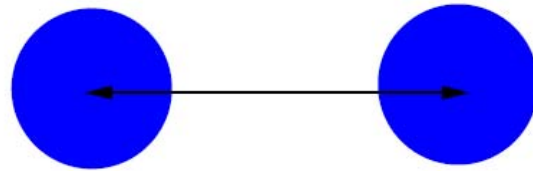
(- - - - exact solution)

QM-AdResS

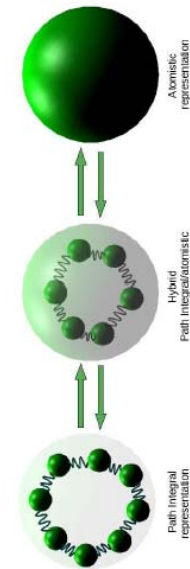
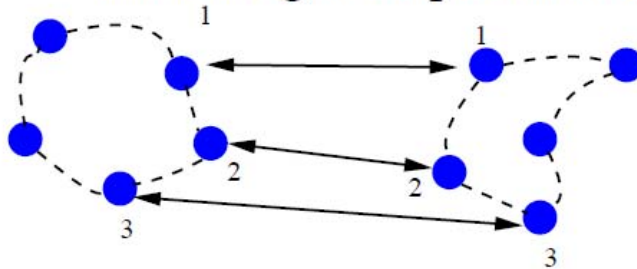
A. Poma, L. Delle Site PRL 2010

Quantum properties based on the delocalization of atoms

Classical Representation



Path Integral Representation

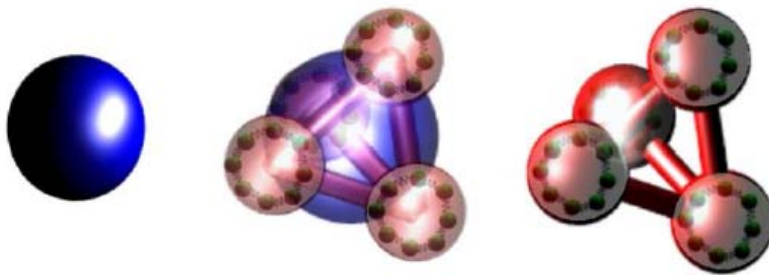


Path Integral (ring polymer) representation of classical atoms

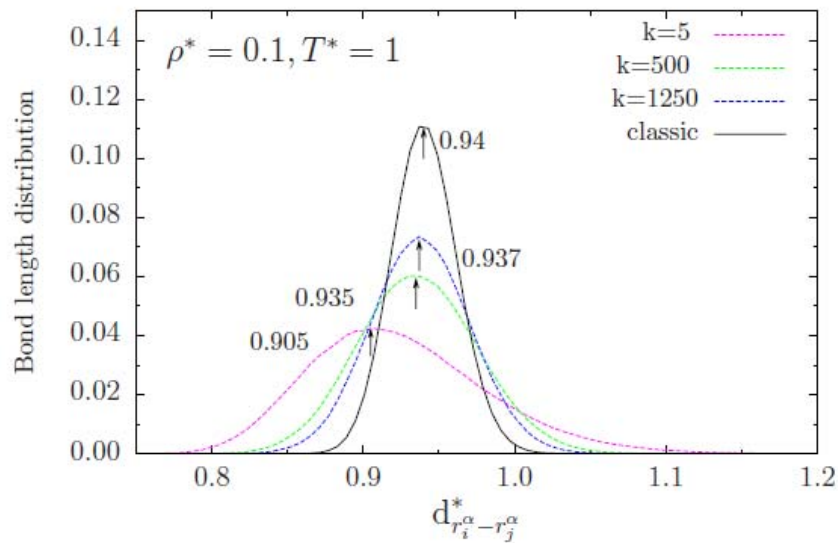
See: M.E.Tuckerman, NIC Series, Vol.10, pg 268 (2002).

QM-AdResS

A. Poma, L. Delle Site PRL 2010

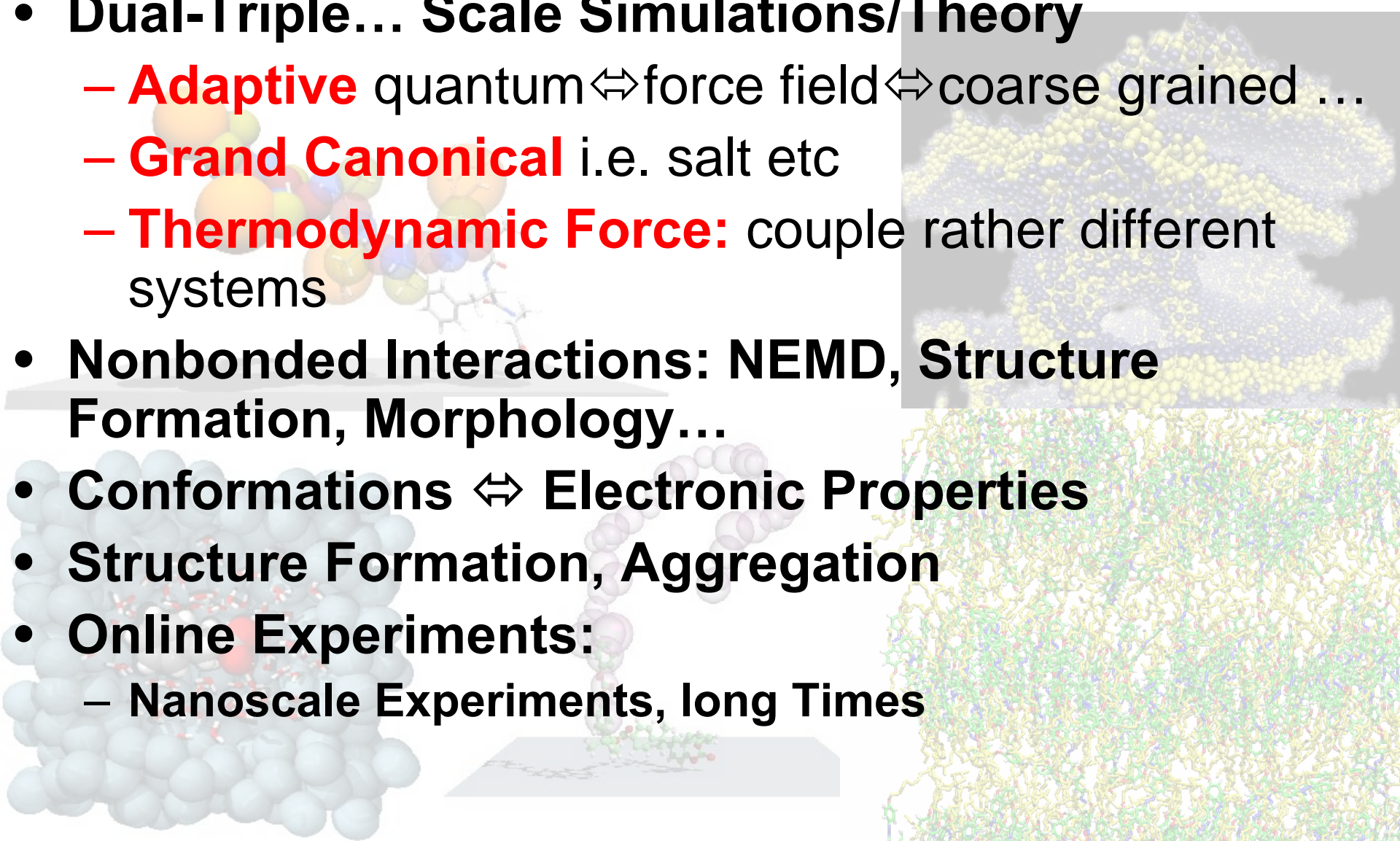


Rigidity of Tetrahedral molecule in PIMD



Conclusion / Challenges

- **Dual-Triple... Scale Simulations/Theory**
 - **Adaptive** quantum \leftrightarrow force field \leftrightarrow coarse grained ...
 - **Grand Canonical** i.e. salt etc
 - **Thermodynamic Force:** couple rather different systems
- **Nonbonded Interactions: NEMD, Structure Formation, Morphology...**
- **Conformations \leftrightarrow Electronic Properties**
- **Structure Formation, Aggregation**
- **Online Experiments:**
 - **Nanoscale Experiments, long Times**



KITP UCSB Program 2012

- **Physical Principles of Multiscale Modeling, Analysis and Simulation in Soft Condensed Matter**
- **Apr 2, 2012 - Jun 29, 2012**
- **Application deadline: August 15, 2011**
- **Coordinators: Paul Atzberger, Kurt Kremer, Mark Robbins**